The Gender Investment Gap over the Life-Cycle

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Abstract

Single women hold less risky portfolios than single men. This paper analyzes the determinants of the "gender investment gap" based on a structural life-cycle framework. The model rationalizes the investment gap without gender heterogeneity in preferences. Rather, lower deterministic income and larger household sizes of single women are the main determinants of the gap. Gender heterogeneity in deterministic income matters because women earn less on average (level effect) and because the income gap is largest early in life, preventing young single women from entering the stock market, thereby perpetuating differences in wealth and participation rates later on (slope effect).

Keywords: Household Finance, Life-Cycle, Gender, Portfolio Choice

JEL: E21, G11, G50, J16

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1 Introduction

Single women are less likely to participate in the stock market than single men and if they do, they allocate a smaller share of their portfolio toward risky assets. In the presence of an equity premium, a less risky portfolio translates (ceteris paribus) into lower wealth levels. This paper studies the sources of the so-called "gender investment gap" based on a structural life-cycle framework. Generally, differences in investment behavior can arise due to differences in circumstances (such as income profiles, number of household members, etc.) or due to differences in unobservable characteristics such as preferences. In fact, there exists a large empirical literature documenting higher degrees of risk aversion for women with regard to financial choices (see for example Eckel and Grossman (2008), Croson and Gneezy (2009), or Charness and Gneezy (2012) for a review) which would be a natural candidate explanation for a lower female equity share.

However, by analyzing the question through the lens of a structural model, I show that such a framework is able to match the empirical gender investment gap without introducing gender heterogeneity in preferences. Rather, lower deterministic income and larger household sizes of single women are the main determinants for explaining the gap. Importantly, both contemporaneous and future outcomes of both variables matter for current-period investment choices. Consequently, reduced form regressions that control for household observable characteristics but do not take into account future outcomes fail to fully explain the empirical gender investment gap.

In the following, I first document life-cycle profiles of asset holdings and portfolio choices for single men, single women, and couples using survey data on U.S. households. My empirical findings confirm the gender investment gap: women are less likely to participate in the stock market and allocate – conditional on participating – a lower share of their portfolio toward risky assets. All differences are statistically different from zero, even after controlling for a wide range of observable characteristics that have been shown to affect investment behavior.

To uncover which factors account for the unexplained part of the gap and to quantify the relative importance of each channel, I develop a life-cycle model of portfolio choice that allows for differences in household structure (single or couple) and gender. Individuals can get married and divorced. Single men and single women differ in their income profiles (both the deterministic and stochastic part), the number of individuals who live in their household (e.g. children), their marital transition probabilities, the (expected) characteristics of their partner in the event of marriage as well as survival probabilities and out-of-pocket medical expenditures during retirement. In contrast, I restrict preference parameters to be identical across all types of households. I calibrate the model using the Survey of Consumer Finances (SCF) for financial choices and the Panel Study of Income Dynamics (PSID) for labor income and demographic characteristics. The model matches well the life-cycle profiles of asset holdings and equity shares for both single men and single women.

By means of counterfactual exercises, I show that gender heterogeneity in deterministic income and the average number of household members are the most important determinants of the gender investment gap. Deterministic income matters both through its level and slope. Single women's deterministic income is lower than that of their male counterparts, making them less likely to participate in risky asset markets. In addition, the gap in deterministic income is largest early in life, preventing single women from participating in the stock market when young. As a result, they earn lower returns in expectation, accumulate less wealth, and become less likely to participate later on. In contrast, heterogeneity in the stochastic component of income contributes to widening the gap.

I then decompose the gender investment gap into a *composition* and *policy* effect. The composition effect explains how much of the gap arises from differences in observable characteristics, that is in the distribution of individuals across the state space. The policy effect describes how much of the gap can be accounted for by differences in policy functions for the equity share conditional on state variables. Since all agents in the model are forward looking, heterogeneity in policy functions (conditional on the state vector) arises from heterogeneity

in future outcomes.

On aggregate, the composition effect (that is, heterogeneity in the sample composition) explains most of the gender gap in participation rates among young households. In contrast, lower female equity shares conditional on participation mainly arise due to gender differences in policy functions.

When further analyzing the importance of individual model elements for the policy effect, I find that lower female deterministic income contributes to single women taking less financial risk, even conditional on state variables. As long as the risky asset has some bond-like characteristics, the optimal equity share is decreasing in the ratio of the present value of human capital (i.e., the present value of future expected income) over current assets (Merton, 1969, 1971). Hence, if a man and woman have the same current net worth (and income), it is optimal for the woman to choose a smaller equity share if her (deterministic) income is lower than that of the man in future periods, that is, if she is endowed with less human capital.

In addition, larger female household sizes – which mainly arise through a higher likelihood of having children living in the same household – affect single women's policy functions both with regard to participation rates and conditional risky shares. Conditional on state variables, larger future household sizes act as a consumption commitment that makes single women more vulnerable to financial shocks. As a result, they reduce financial risk-taking.

Lastly, I provide direct empirical support for the model mechanisms. First, I show that controlling for proxies of deterministic income (as opposed to overall income) further reduces the gender investment gap in the data. Second, by complementing the analysis with data from the New York Fed Survey of Consumer Expectations, I show that single women expect lower future earnings and more non-spousal household members than single men. Hence, singles in the data are aware of gender heterogeneity in future outcomes, even after controlling for current observable characteristics.

While the focus of the paper is on stock market investment, its implications go beyond this specific application. A large literature has documented that women earn less in real estate markets and choose less risky portfolio compositions in retirement accounts. Beyond financial markets, there exists evidence that women, and in particular single mothers, sort into less risky occupations, changing their trajectory of lifetime earnings (e.g. Bertrand, 2011, DeLeire and Levy, 2004). Dohmen, Falk, Huffman, Sunde, Schupp, and Wagner (2011) combine survey and experimental evidence to show that women behave more risk averse with regard to career choices and financial outcomes. In turn, lower asset returns have been linked to slower wealth accumulation and financial vulnerability of women, especially during old age (e.g. Neelakantan and Chang, 2010, Goldsmith-Pinkham and Shue, 2023).

However, to correctly design and evaluate policies that aim at promoting female financial security, it is important to understand whether gender differences in risk-taking arise from underlying variation in preferences or from societal constraints that result in women making less risky choices.² If differences are purely preference-driven, both men and women behave optimally without any room for welfare improvements. In contrast, if women face different constraints than men, removing these constraints can change women's perception about their lifetime income trajectory or future consumption commitments and subsequently result in more risky investments and faster wealth accumulation in expectation.

A similar argument applies to the correct cost-benefit evaluation of such policies. For example, the impact of a policy that aims at closing the gender wage gap on female wealth accumulation gets amplified by encouraging women to invest in more risky assets that pay on average higher returns. Hence, the implementation of such a policy may be less costly than previously assumed as it generates higher (capital) tax revenues and further weakens

See e.g. Sunden and Surette (1998), Agnew, Balduzzi, and Sunden (2003), Arano, Parker, and Terry (2010), Säve-Söderbergh (2012) on retirement accounts and Andersen, Marx, Nielsen, and Vesterlund (2021), Girshina, Bach, Sodini, and Team (2022), Goldsmith-Pinkham and Shue (2023) on gender gaps in real estate markets.

² Such policies may include more generous child support payments for single parents, subsidized childcare, but also programs directed at promoting women's career and income progression (e.g. female quotas).

women's dependence on government transfers, in particular during old age.

Related Literature. This paper contributes to several strands of the literature. First, it adds to a literature documenting gender differences in investment behavior and financial choices. There is widespread consensus that women invest less risky than men. Jianakoplos and Bernasek (1998) document lower equity shares among single women than single men in U.S. data. Sunden and Surette (1998) and Agnew et al. (2003) show that women in the U.S. choose lower equity allocations in retirement saving plans. Arano et al. (2010) cannot confirm significant gender differences in retirement accounts for U.S. single households but do so for married individuals. Barber and Odean (2001) find that single men trade more often in risky assets and attribute this result to male overconfidence. Säve-Söderbergh (2012) documents that even though women do not exclude stocks more frequently from their pension contribution plan, they allocate a smaller share into risky assets. Almenberg and Dreber (2015) and Thörnqvist and Olafsson (2019) show that the gender investment gap in Sweden prevails until today. Ke (2018) attributes cross-country differences in stock market participation rates to gender norms, showing that countries with strong gender norms exhibit lower female participation rates. Moreover, several papers document that women earn lower returns in real estate markets (Andersen et al., 2021, Girshina et al., 2022, Goldsmith-Pinkham and Shue, 2023). My paper adds to this literature by being the first work to analyze the gender investment gap through the lens of a structural framework.

Second, this paper relates to an experimental literature which finds that women choose less risky portfolio allocations in investment games (Eckel and Grossman, 2008, Croson and Gneezy, 2009, Charness and Gneezy, 2012) as well as to survey evidence documenting that women rate their willingness to take risk lower than men, even after controlling for a wide range of observable characteristics (e.g. Dohmen et al., 2011). Both findings can lead to the conclusion that women are more risk averse than men. At first, my results seem to contradict this literature because my model replicates the gender investment gap without introducing heterogeneity in risk aversion. However, also with model simulated data, reduced form re-

gressions that control for observable characteristics fail to fully explain the gender investment gap. The structural analysis reveals that both current and future deterministic income and household sizes can explain the observed gap in investment choices, rather than innate differences in risk aversion. Hence, my paper confirms prior results on gender heterogeneity in risk-taking, it simply differs in the interpretation of the underlying sources that drive these patterns.

Third, I relate to a literature that explores how family-related shocks affect portfolio allocation and savings. Cubeddu and Ríos-Rull (2003) study the role of marriage and divorce on wealth accumulation in a dynamic setting. Love (2010) was the first paper to present a joint life-cycle framework of marital status and portfolio choice. He finds that married investors hold more risky portfolios than singles. In the event of divorce, stock holdings increase for men whereas they decline for women. Hubener, Maurer, and Mitchell (2015) extend the analysis by incorporating endogenous labor supply and realistically calibrated social security benefits. Christiansen, Joensen, and Rangvid (2015) empirically address the heterogeneous impact of family shocks on portfolio choices across gender using administrative panel data from Denmark. Similar to Love (2010) for the U.S., their findings suggest that the fraction of risky assets in women's portfolios increases after marriage whereas it declines after divorce. For men, this relationship points in the opposite direction. Along the same lines, Bertocchi, Brunetti, and Torricelli (2011) find in an empirical framework that the marital gap of stock holdings in Italy is larger for women than men. While all these papers show that family-related shocks affect portfolio choices heterogeneously across gender, neither of them quantifies the importance of such shocks for gender differences in investment behavior over the life-cycle.

More broadly, my paper extends a literature that studies life-cycle patterns of household finances. For a literature review, see Poterba and Samwick (2001) and Gomes (2020). Typically, life-cycle models of portfolio choice predict very high participation rates and equity shares to be strongly declining in age, which is at odds with the data. The literature has

proposed several mechanisms to explain this discrepancy. The most prominent ones are costs associated with stock market investment (Vissing-Jorgensen, 2002, Gomes and Michaelides, 2005, Alan, 2006), the illiquid nature of housing (Cocco, 2005), lack of financial literacy (Lusardi and Mitchell, 2014), or accounting for cyclicality of higher order moments in the income process (Catherine, 2022, Shen, 2023). However, so far little focus has been on marital transitions as an additional source of financial uncertainty that limits the propensity to take risk in the stock market.

Roadmap. The remainder of the paper is structured as follows. Section 2 presents empirical observations on gender-specific portfolio choices. Section 3 introduces the structural model. Section 4 presents the calibration strategy and Section 5 shows the quantitative results. In Section 6, I analyze the mechanisms that drive the model results. Section 7 performs several robustness checks and Section 8 concludes.

2 The Gender Investment Gap in the Data

The following section first describes the data and sample selection criteria. Next, I document empirical patterns of portfolio choices for single men, single women, and couples over their life-cycle.

2.1 The Sample

I use the waves from 1989 until 2016 of the Survey of Consumer Finances (SCF) to measure portfolio choices of households. I restrict the sample to individuals between 30 and 65 years. The SCF is a triennial repeated cross-sectional survey sponsored by the Federal Reserve Board. It is carried out at the household level but collects individual demographic characteristics and income variables as well as detailed information on joint asset holdings.

For income variables and demographic characteristics, I work with data from the Panel Study of Income Dynamics (PSID) spanning from 1989 until 2017 (Panel Study of Income

Dynamics, 2021). The PSID is a longitudinal panel survey of private households in the U.S. running from 1968 until today.³ Besides the core sample, the PSID oversamples low-income families (the 'SEO' sample) and immigrant families (the 'immigrant' sample).

I combine two datasets for my analysis because I need detailed portfolio choice information and panel data on household income (to estimate the income processes). Unfortunately, while the SCF collects the former, it does not follow the same household over time. In contrast, asset information in the PSID is only reported in some waves and lacks precise information on the portfolio composition of the household. To nevertheless increase confidence in the comparability of the sample across datasets, I show in Appendix A.1 that life-cycle profiles of variables that are available in both datasets look very similar.⁴

To ensure the representativeness of the U.S. population, I drop all families belonging to the two sub-samples in the PSID and weigh each observation by the provided survey weights in both datasets. All financial variables are converted into 2007 dollars using the CPI-U and winsorized at the 1^{st} and 99^{th} percentile.

I define a single woman to be a family unit with a female head and no spouse present. Single men are defined accordingly. Couples include legally married and cohabiting households. In total, the PSID sample consists of 100,907 individual-year observations (82,705 for couples, 7,057 for single men, and 11,145 for single women) that correspond to 2,091 unique single women, 1,624 unique single men, and 11,376 individuals who live in couples. The SCF includes information on 23,496 individuals in couples, 4,088 single men, and 6,155 single women.

³ Because the Survey of Consumer Finances starts in 1989, I restrict my data sample taken from the PSID to the waves from 1989 until 2017. Data was collected annually until 1997 and afterwards every two years.

⁴ Combining multiple datasets to estimate structural models is not uncommon in the literature. For instance, Cooper and Zhu (2016) combine the PSID and SCF to estimate the effect of education on stock market investment. Borella, De Nardi, and Yang (2023) use the PSID together with the Health and Retirement Study (HRS) to study lifetime outcomes during working life and retirement.

2.2 Life-Cycle Profiles of Portfolio Allocation

Net worth is defined as total assets minus total debt. Total assets include financial assets, real estate, and vehicles. Total debt consists of mortgages, credit card balances, installment loans (e.g. education or vehicle loans), as well as other forms of debt such as loans against pensions or life insurances. Risky assets include direct stock holdings, corporate and foreign bonds, the fraction of mutual funds that include the former, as well as the fraction of retirement accounts which is invested in stocks.⁵

Figure 1a displays the life-cycle profiles of equity shares for single men, single women, and couples.⁶ The equity share is defined as the fraction of net worth that is invested in risky assets. It combines the extensive margin (whether or not the household owns any risky assets) with the intensive margin (conditional on holding risky assets, what share of net worth is allocated to them). Figure 1b and Figure 1c separately plot the stock market participation rate and conditional risky share. The gender difference in equity shares is statistically different from zero, in particular during young age, as displayed by the confidence bands and corresponding regression coefficients in Table 1. However, it seems that the gender investment gap is primarily driven by lower participation rates of single women, as opposed to lower risky shares conditional on participation (Figures 1b and 1c).

On average, the equity share of single women is around 4.5%-points lower than that of single men which – given an average male equity share of 15% – corresponds to being ca. 30% lower. Moreover, both the gender gap in equity shares and stock market participation rates converge toward the entry of retirement.

As indicated by the black solid line in Figure 1a, couples have on average a higher equity share than singles which is driven by the extensive margin (see the black solid lines in Figures

⁵ In Appendix A.2, I show that my results are robust to adopting a tighter definition that excludes risky assets held through retirement accounts.

⁶ To account for cohort effects, Appendix A.2 replicates Figure 1 for individuals born within a relatively short time-frame.

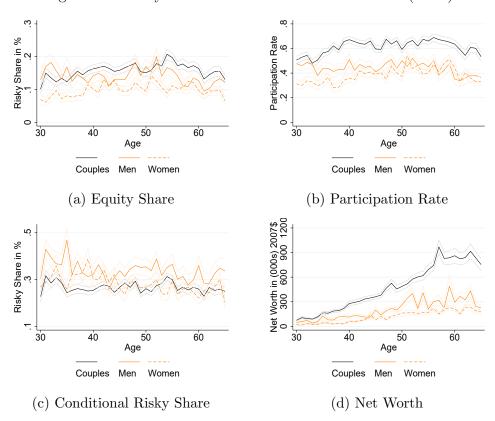


Figure 1: Life-Cycle Patterns of Household Finances (Data)

Notes: Figure 1 plots the life-cycle profiles of equity shares, stock market participation rates, conditional risky shares, and net worth for singles and couples, including 95% confidence intervals. All figures display averages of the pooled sample by age and household type. Data is from the waves 1989 until 2016 of the Survey of Consumer Finances (SCF). Risky assets are defined as direct stock holdings, corporate and foreign bonds, the fraction of mutual funds that include the former, and the fraction of retirement accounts which is invested in stocks.

1b and 1c, respectively). This finding is partly mechanical as couples are composed of two individuals for whom I compute the joint probability of participation. If I randomly draw a single man and a single woman and compute the likelihood that at least one of them holds risky assets (conditional on age), the participation rate of such a "generated couple" closely aligns with the one of couples in the data.

Figure 1d confirms that single women accumulate less net worth than single men. This gap is often referred to as the "gender wealth gap". Throughout their working life, the gap in net worth is on average \$87,000 and diverges as households grow older.

2.3 Regression Coefficients over the Life-Cycle

The empirical gender differences in portfolio choices reported in Figure 1 can arise due to differences in circumstances or preferences. As a first exercise to quantify the importance of the former, Table 1 reports the results of reduced form regressions that control for household observable characteristics. I run Tobit regressions (to account for non-participating households) of the equity share on a gender dummy, age polynomials, and gender interacted with age (Column (1)). In Column (2), I additionally control for observable characteristics that have shown to be important predictors of portfolio choices. Following Christelis, Georgarakos, and Haliassos (2013), I control for the education of the individual, the overall number of household members, the inverse hyperbolic sine transformation of non-asset income, and year fixed-effects.⁷ Column (3) furthermore includes the inverse hyperbolic sine transformation of households' safe assets, which are defined as all net worth that is not invested in risky assets. Column (4) additionally controls for occupation and industry fixed effects. The corresponding marginal effects of being a single woman along with their standard errors at various ages are reported in the last three rows of Table 1.8

The coefficient for being a single woman is negative (and statistically significant) across all specifications and becomes smaller as I include more controls. Similarly, the interaction term of gender and age is largest in the first column (least controls) and declines across columns. When considering the marginal effect of being a single woman ("ME"), I find a negative and significant gender effect across all four columns. However, as individuals age, this "negative" effect of being a woman on the equity share becomes smaller and, for some specifications, turns insignificant.

Thus, the unexplained part of the gender investment gap (i.e., the part that is not accounted for by household observable characteristics) is strongest among young households and declines

Non-asset income includes labor earnings, social security benefits, welfare payments, income from unemployment or worker's compensation, as well as child support and alimony payments.

⁸ Appendix A.4 reports the corresponding specifications separately for the participation rate and conditional risky share.

along the life-cycle. To further explore which factors are driving this unexplained part and to quantify their relative importance, Section 3 builds a structural model of gender and portfolio choice. Having a structural model helps to accommodate non-linearities and account for factors that cannot be easily controlled for in reduced form specifications, such as future outcomes of variables.

3 A Life-Cycle Model of Portfolio Choice

In this section, I develop a stochastic life-cycle model with women and men (denote gender by $i = \{f, m\}$) who live either as singles (\mathcal{S}) or married couples (\mathcal{M}). Life is split into two stages: working age and retirement. Time is discrete and the model period is one year. Agents start their life at age 30, retire at 65, and live at most until age 85, i.e., $j \in \{30, 31, ..., 65, ..., 85\}$. At age 30, agents are ex-ante heterogeneous in terms of education θ which can take two values ($\theta = \{l, h\}$) and refers to having at least 12 years of schooling or not in the data.

During working age, households are subject to uninsurable labor income shocks that depend on their gender, marital status, and the aggregate state of the economy. When being single, individuals decide how much to consume (c_i) , how much to save in a safe asset (a_i^s) , and how much to save in a risky asset (a_i^r) . While the risky asset pays an equity premium, its return is uncertain and varies with the aggregate state. Couples decide jointly on the level of consumption $(c_{\mathcal{M}})$ and how much to save in both types of assets $(a_{\mathcal{M}}^s, a_{\mathcal{M}}^r)$. Singles face an exogenous marriage probability that depends on their gender, age, and education. Likewise, couples face an exogenous divorce probability that varies by age and both spouses' education.

During retirement, agents face age- and gender-dependent medical expenditures and are subject to longevity risk. Upon dying, agents value leaving bequests. As during working age, they can live either as singles or couples. However, their marital status is fixed. If one spouse living in a couple dies, the surviving spouse continues his or her life as a single with a

⁹ I abstract from modeling housing explicitly. See Appendix B for details.

Table 1: Regression Coefficients & Marginal Effects – Equity Shares of Singles

	(1) Equity Share	(2) Equity Share	(3) Equity Share	(4) Equity Share
single woman	-0.3347^{\diamond} (0.0131)	-0.2136^{\diamond} (0.0109)	-0.1665^{\diamond} (0.0121)	-0.1211^{\diamond} (0.0140)
single woman*age	0.0051^{\diamond} (0.0002)	0.0032^{\diamond} (0.0002)	0.0026^{\diamond} (0.0002)	0.0014^{\diamond} (0.0002)
age	-0.0988^{\diamond} (0.0135)	-0.0508° (0.0147)	-0.0482° (0.0166)	-0.0294 (0.0186)
age^2*100	0.2442^{\diamond} (0.0292)	0.1354° (0.0319)	0.1185° (0.0357)	0.0760 (0.0409)
$age^3 * 10000$	-0.1936^{\diamond} (0.0206)	-0.1120^{\diamond} (0.0224)	-0.0965° (0.0251)	-0.0602^{\diamond} (0.0292)
high education		0.2676^{\diamond} (0.0020)	0.2449° (0.0018)	0.1297^{\diamond} (0.0042)
number of HH members		-0.0554° (0.0017)	-0.0557° (0.0020)	-0.0507^{\diamond} (0.0030)
non-asset income		0.0365^{\diamond} (0.0007)	0.0326^{\diamond} (0.0007)	0.0283° (0.0007)
safe assets			0.0217^{\diamond} (0.0012)	0.0146° (0.0009)
constant	1.2071^{\diamond} (0.2027)	-0.0845 (0.2177)	-0.1669 (0.2403)	-0.4190 (0.2751)
Observations Year FE Industry & Occupation FE	10,243 No No	10,239 Yes No	10,239 Yes No	7,606 Yes Yes
ME for women at age 30	-0.1811° (0.0065)	-0.1170° (0.0060)	-0.0888 ^{\disp} (0.0063)	-0.0783° (0.0075)
ME for women at mean age (47)	-0.0921^{\diamond} (0.0032)	-0.0610^{\diamond} (0.0036)	-0.0438^{\diamond} (0.0034)	-0.0555^{\diamond} (0.0042)
ME for women at age 65	-0.0018 (0.0031)	-0.0042 (0.0028)	0.0019 (0.0032)	-0.0283° (0.0017)

Notes: Estimations are based on Tobit regressions on the sample of individuals who live in households with no spouse present. Source: SCF waves 1989 until 2016. Equity Share = Unconditional risky share, with the risky share being defined as the fraction of net worth that is invested in risky assets. $single\ woman$ is a dummy indicating that the household head is a woman. $high\ education$ is a dummy equal to one if the household head has more than 12 years of education. $safe\ assets$ refers to all net worth that is not invested in risky assets. "ME" indicates the marginal effect of being a woman at the respective age. Robust standard errors in parentheses, \diamond p<0.05.

fraction of the couple's assets. As before, households have a portfolio choice between a safe and risky asset.

3.1 Preferences

All households have time-separable CRRA preferences over a consumption good c. The period flow of utility for singles and couples is given by:

Singles:
$$u(c) = \frac{\eta_{ij} \left(\frac{c}{\eta_{ij}}\right)^{1-\gamma}}{1-\gamma}$$
 Couples: $u(c) = \frac{\eta_{\mathcal{M}j} \left(\frac{c}{\eta_{\mathcal{M}j}}\right)^{1-\gamma}}{1-\gamma}$

where γ is the coefficient of relative risk aversion and η is an equivalence scale that adjusts for household size. The term η is allowed to vary by age j and family type (couple, single man, single woman).

Bequest Motive. In the event of death, individuals derive utility from leaving bequests according to:

$$\phi(a') = L \frac{(\omega + a')^{1-\gamma}}{1-\gamma}$$

where a' denotes the bequeathed assets, ω captures the luxuriousness of the bequest motive and L governs the bequest intensity. Couples value leaving bequests if they both die within the same period. Whenever only one spouse dies, the surviving spouse continues life as a single and values leaving bequests in the case of his or her own death.

3.2 Dynamics

Aggregate State. The economy is characterized by an aggregate state Ω that governs labor market conditions and stock returns, as explained in detail below. The aggregate state can take two values, referring to booms and recessions ($\Omega = \{b, r\}$). Recessions realize with probability p_{rec} and are not persistent.

Asset Returns. The safe asset pays a time-invariant return r_s . The return of the risky

asset depends on the aggregate state Ω and follows a mixture normal distribution:

$$r_r = \begin{cases} \mathcal{N} \sim (\mu_r^{\text{boom}}, \sigma_r^2) & \text{if } \Omega = b \text{ with probability } (1 - p_{\text{rec}}) \\ \mathcal{N} \sim (\mu_r^{\text{rec}}, \sigma_r^2) & \text{if } \Omega = r \text{ with probability } p_{\text{rec}} \end{cases}$$

In expectations, the risky asset pays an equity premium and it holds that $\mu_r^{\text{boom}} > \mu_r^{\text{rec}}$.

Income Profiles. The income profiles are allowed to vary between singles and couples. Conditional on marital status, income y_{ij} at age j for gender i can be split into a deterministic and stochastic component and is expressed as:

$$y_{ij} = \bar{y}_i \theta_i \xi_{ij} \tilde{y}_{ij}(\Omega)$$

The term \bar{y}_i denotes a constant, θ_i is the (exogenous) education premium, and ξ_{ij} stands for an age-specific component. The term $\tilde{y}_{ij}(\Omega)$ represents the stochastic component of income and consists of a transitory and persistent part, with the latter being allowed to vary with the aggregate state Ω . In particular,

$$\tilde{y}_{ij} = z_{ij} + \epsilon_{\tilde{y}ij} \quad \text{with} \quad z_{i,j} = \begin{cases} \mu_z^{\text{boom}} + \rho_{zi} z_{i,j-1} + \nu_{zij} & \text{if } \Omega = b \text{ with probability } (1 - p_{\text{rec}}) \\ \mu_z^{\text{rec}} + \rho_{zi} z_{i,j-1} + \nu_{zij} & \text{if } \Omega = r \text{ with probability } p_{\text{rec}} \end{cases}$$

The terms $\epsilon_{\tilde{y}ij}$ and ν_{zij} are independent zero mean random shocks with variances $\sigma_{\tilde{y}i}^2$ and σ_{zi}^2 , respectively. The parameter $\rho_{zi} \in (0,1]$ captures the persistence of shock ν_{zi} . To keep the process stationary, I impose that $\mu_z^{\text{boom}} = \left(\frac{-p_{\text{rec}}}{1-p_{\text{rec}}}\right)\mu_z^{\text{rec}}$. Neither μ_z^{boom} nor μ_z^{rec} is allowed to vary by gender or marital status.

Within couples, the transitory shocks $\epsilon_{\tilde{y}fj}$ and $\epsilon_{\tilde{y}mj}$ are assumed to be correlated (with $\rho_{\sigma_{\tilde{y}f},\sigma_{\tilde{y}m}} = 0.3$). Spouses live in the same area and are likely to work in similar industries and

are thus subject to correlated labor market shocks.¹⁰ Lastly, I follow Huggett and Kaplan (2016) and impose a flat labor income tax rate $\tau = 0.27$.

Out-of-Pocket Medical Expenditures. When being retired, agents are subject to medical expenditures m_{ij} that are a deterministic function of age and gender. Because individuals face survival risk and medical expenditures are strictly increasing in age, deterministic medical expenditures impose a risk in that agents are uncertain whether they live until the age when have to pay the medical bills. This modeling choice is motivated by De Nardi, French, and Jones (2010) who show that the main sources of risk during retirement are not fluctuations of medical expenditures around their mean but rather their age-dependent level combined with longevity risk.

Marriage and Divorce. Singles get married with an exogenous probability $\mu(i, j, \theta)$ that depends on their gender i, age j, and education θ . Conditional on meeting a partner, the probability of meeting a partner with education θ_p and income shock realization \tilde{y}_p is defined as $\Pi(.) = \Pi(\theta_p, \tilde{y}_p | \theta_i, \tilde{y}_i)$. Both partners have the same age. Individuals are always matched to a partner with the mean empirical amount of assets conditional on age, gender, and education. This specification generates assortative mating along asset holdings close to the data. Couples face an exogenous divorce probability that depends on age and education of both spouses $\lambda(j, \theta_f, \theta_m)$. Upon divorce, assets are split equally with 10% being exogenously destroyed to account for costs of a marital dissolution.¹¹ There are no alimony payments.

3.3 Stock Market Participation Cost

Agents have to pay a fixed cost S_j^F each period if they choose to invest part of their savings in the risky asset. I allow for the possibility that this cost varies by age j. For example, as Catherine (2022) notes, young households may face lower costs because they are automatically

¹⁰ By setting the correlation to 0.3, I follow Borella et al. (2023) who estimate an empirical correlation between initial wage draws for newly formed couples in U.S. data of 0.22 for the age group 25-34, 0.36 for ages 35-44, and 0.42 for couples above 45 years.

 $^{^{11}}$ This splitting rule is motivated by the data. In the PSID, the median fraction of singles' financial wealth one period after a divorce is 45% of the former couple's wealth, regardless of the individual's gender.

enrolled in retirement plans or tend to be more financially literate. Moreover, following Vissing-Jorgensen (2002), participation costs have to be paid each period irrespective of the history of stock holdings. The main advantage of modeling participation costs as a flow variable rather than an entry cost (see e.g. Alan (2006) or Cooper and Zhu (2016)) is that flow costs do not require introducing stock holdings as a state variable.

3.4 Timing

At the beginning of period t, households learn their current productivity state(s), marital status, and asset level (which depends on their stock market return). Thus, agents start period t with a given amount of assets that depends on their decisions in period t-1, marital status, and the realization of the risky asset return. After observing all shock realizations, agents decide on how much to consume and save in both the risky and safe asset. When investing part of their endowment in the risky asset, they have to pay the stock market participation costs S_j^F in the current period t.

3.5 Recursive Formulation

I express the problem recursively by defining six value functions: the value function for singles, the value function for couples, and the value function for an individual living in a couple, all during working age and retirement. The latter is the relevant object when computing the present value of marriage for a single whereas the value function for couples determines the optimal allocation of resources within couples across time (Borella, De Nardi, and Yang, 2020). Because the stock market participation cost has to be paid per period and given the i.i.d. nature of the risky asset and aggregate state, I can combine labor income with safe and risky assets into one "cash-on-hand" variable: $a = (1 - \tau)y(j, \theta, \tilde{y}(\Omega)) + (1 + r_r(\Omega))a_r + (1 + r_s)a_s$.

Singles – Working Age. The state variables of a single agent are her gender i, age j, education θ , cash-on-hand a, and current income realization \tilde{y} . The corresponding value

function reads as:

$$V^{S}(i, j, \theta, a, \tilde{y}) = \max_{a'_{s} \geq 0, a'_{r} \geq 0, c \geq 0} \frac{\eta_{ij} \left(\frac{c}{\eta_{ij}}\right)^{1-\gamma}}{1-\gamma} + (1 - \mu(i, j, \theta))\beta \mathbb{E}V^{S}(i, j + 1, \theta, a', \tilde{y}') + \mu(i, j, \theta)\beta \mathbb{E}\hat{V}^{C}(i, j + 1, \theta, \theta_{p}, a' + a'_{p}, \tilde{y}', \tilde{y}'_{p})$$

subject to:

$$a'_r + a'_s + c = a - \mathbb{1}_{a'_r > 0} S_j^F$$
 with $a = (1 - \tau)y(j, \theta_i, \tilde{y}_i(\Omega)) + (1 + r_r(\Omega))a_r + (1 + r_s)a_s$

The labor income and risky return process are defined in Section 3.2. The term η_{ij} denotes an equivalence parameter that controls for changing family size over the life-cycle. \hat{V}^C expresses the value of individual i of getting married to partner p. Single individuals take the expected value over future productivity realizations, asset returns, and the realization of the aggregate state when staying single whereas they form expectations over future productivity realizations, asset returns, the aggregate state, and their specific partner in case of getting married.

Singles – Retirement. The state variables of a retired single are her gender i, age j, education level θ , cash-on-hand a, and the last income realization before retirement (\hat{y}) .

$$V_{R}^{S}(i, j, \theta, a, \hat{y}) = \max_{a_{s}' \geq 0, a_{r}' \geq 0, c \geq 0} \frac{\eta_{ij} \left(\frac{c}{\eta_{ij}}\right)^{1-\gamma}}{1-\gamma} + \beta \psi_{ij} \mathbb{E} V_{R}^{S}(i, j+1, \theta, a', \hat{y}) + \beta (1-\psi_{ij}) L \frac{\left(\omega + a'\right)^{1-\gamma}}{1-\gamma}$$

subject to:

$$a'_r + a'_s + c = a - m_{ij} - \mathbb{1}_{a'_r > 0} S_i^F$$
 with $a = (1 - \tau) pen_s(\hat{y}) + (1 + r_r(\Omega)) a_r + (1 + r_s) a_s$

The return process for the risky asset is defined in Section 3.2. The terms ψ_{ij} and m_{ij} denote age- and gender-dependent survival probabilities and medical expenditures. Retired singles

take the expected value over asset returns, realization of the aggregate state, and likelihood of survival.

Couples – Working Age. The state variables of a couple that consists of a woman f and man m can be summarized by their age j, education of both spouses θ_f, θ_m , joint cash-onn-hand a, and both productivity realizations \tilde{y}_f, \tilde{y}_m . The corresponding value function reads as:

$$V^{C}(j, \theta_f, \theta_m, a, \tilde{y}_f, \tilde{y}_m) = \max_{a'_s \ge 0, a'_r \ge 0, c \ge 0} \frac{\eta_{\mathcal{M}j} \left(\frac{c}{\eta_{\mathcal{M}j}}\right)^{1-\gamma}}{1-\gamma} + (1 - \lambda(j, \theta_f, \theta_m))\beta \mathbb{E}V^{C}(j+1, \theta_f, \theta_m, a', \tilde{y}'_f, \tilde{y}'_m) + \lambda(j, \theta_f, \theta_m)\beta \sum_{i=f,m} \mathbb{E}V^{S}(i, j+1, \theta_i, 0.9 \frac{a'}{2}, \tilde{y}'_i)$$

subject to:

$$a'_r + a'_s + c = a - \mathbb{1}_{a'_r > 0} S_j^F$$
 with $a = \sum_{i=f,m} (1 - \tau) y(j, \theta_i, \tilde{y}_i(\Omega)) + (1 + r_r(\Omega)) a_r + (1 + r_s) a_s$

Couples take the expected value of both partners' future productivity realizations, the realization of the aggregate state, and joint asset return when staying married as well as the respective individual's productivity realizations, asset returns, and the aggregate state when getting divorced. The return processes for the risky asset and labor market outcomes are defined in Section 3.2.

Couples – **Retirement.** The value function of a retired couple reads as:

$$\begin{split} V_{R}^{C}(j,\theta_{m},a,\hat{y}_{m}) &= \max_{a'_{s} \geq 0, a'_{r} \geq 0, c \geq 0} \frac{\eta_{\mathcal{M}j} \left(\frac{c}{\eta_{\mathcal{M}j}}\right)^{1-\gamma}}{1-\gamma} + \beta \psi_{jf} \psi_{jm} \mathbb{E} V_{R}^{C}(j+1,\theta_{m},a',\hat{y}_{m}) \\ &+ \beta \sum_{i=f,m} \psi_{ij} (1-\psi_{-ij}) \mathbb{E} V_{R}^{S}(i,j+1,\theta_{m},\delta_{i}a',\hat{y}_{m}) \\ &+ \beta (1-\psi_{jf}) (1-\psi_{jm}) L \frac{(\omega+a')^{1-\gamma}}{1-\gamma} \end{split}$$

subject to:

$$a'_r + a'_s + c = a - \sum_{i=f,m} m_{ij} - \mathbb{1}_{a'_r > 0} S_j^F$$
 with $a = (1 - \tau) pen_c(\hat{y}_m) + (1 + r_r(\Omega)) a_r + (1 + r_s) a_s$

Retired couples take the expected value over the aggregate state, asset return, and individual survival probabilities, with the return process for the risky asset being defined in Section 3.2.

Value to an individual of becoming a couple. The value of an individual in a couple is the relevant object when computing the value of single i for getting married to partner p, i.e., the present discounted value of the individual's utility in the event of marriage (Borella et al., 2020). Variables denoted with a \hat{hat} indicate optimal allocations computed with the value function for couples, given the respective state variables. The value of an individual in a retired couple \hat{V}_R^C is defined accordingly.

$$\hat{V}^{C}(i, j, \theta_{i}, \theta_{p}, a, \tilde{y}_{i}, \tilde{y}_{p}) = \frac{\eta_{\mathcal{M}j} \left(\frac{c}{\eta_{\mathcal{M}j}}\right)^{1-\gamma}}{1-\gamma} + (1 - \lambda(j, \theta_{i}, \theta_{p}))\beta \mathbb{E} \hat{V}^{C}(i, j+1, \theta_{i}, \theta_{p}, a', \tilde{y}'_{i}, \tilde{y}'_{p}) + \lambda(j, \theta_{i}, \theta_{p})\beta \mathbb{E} V^{S}(i, j+1, \theta_{i}, 0.9 \frac{a'}{2}, \tilde{y}'_{i})$$

4 Estimation & Calibration

I estimate and calibrate the model in a two-step strategy following Gourinchas and Parker (2002) and Cagetti (2003). First, I estimate all parameters that can be cleanly identified from the data and pre-set some parameters to values from the literature. In the second step, I calibrate the remaining structural parameters using the Simulated Method of Moments (SMM), taking the parameters from the first stage as given.

4.1 First Stage Estimation

Income Profiles. Figure 2 shows the life-cycle profiles of the deterministic income component by gender and marital status from the PSID. Income is expressed as annual income out

of labor earnings (including labor income from farms and businesses), social security benefits, and transfers (including child support and alimony payments). For singles, I include labor earnings, social security benefits, and transfers from all members of the household. For couples, I assign each spouse their own labor income, social security benefits, transfers, and add half of that from other household members. Moreover, I winsorize the top and bottom percentile of earnings and drop observations who, according to the described measure, report zero annual income (in the case of couples, if they report zero overall income).

I follow Borella et al. (2020) and first split the sample by marital status and then separately regress the inverse hyperbolic sine of income for an individual of gender i at age j,

$$income_{ij} = \alpha + \beta_1 age_{ij} + \beta_2 age_{ij}^2 + \beta_3 woman_i * age_{ij} + \delta_i + u_{ij}$$

on a fixed effect δ_i , age, age^2 , and an interaction term of gender and age. To obtain shifters for gender and education, I regress the sum of the fixed effect and residual on fully interacted dummies of gender and education level:

$$\delta_i + u_{ij} \equiv w_{ij} = \gamma_0 + \gamma_1 woman_i + \gamma_2 educ_i + \gamma_2 woman_i * educ_i + \epsilon_{ij}$$

where $educ_i$ is a dummy taking the value one if the respective individual has more than 12 years of schooling.

The coefficients from these income equations (reported in Table 11 in Appendix C.2) inform me about the deterministic income component in the model. Note that parts of the estimated age gradients are driven by variation in hours worked and transitions in and out of the labor force, as opposed to differences in wages. For example, Borella et al. (2023) document that average hours worked of single women between age 30 and 45 grow faster than those of

¹² In some waves, the PSID does not separately report transfer income or social security benefits for spouse and household head. In these cases, I allocate half of the overall reported measure to the wife and the other half to the husband.

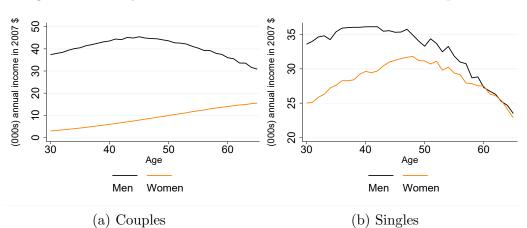


Figure 2: Life-Cycle Profiles of the Deterministic Income Component

Notes: Figure 2 plots the life-cycle profiles for the deterministic income component by gender and marital status. Data is from the waves 1989 until 2016 of the Panel Study of Income Dynamics (PSID).

single men, whereas single men are more likely to drop out of the labor force beyond age 45, contributing to the life-cycle patterns for single households (Figure 2b).

I estimate the parameters governing the stochastic component of the income process using the minimum distance estimator from Guvenen (2009).¹³ Table 2 summarizes the results. My point estimates imply a slightly less persistent income process for single women than for single men (i.e., when comparing the first two columns), whereas the variance of both the persistent shock σ_z^2 and transitory shock $\sigma_{\bar{y}}^2$ is lower for single women. That is, the overall variance of single women's income process is lower than that of single men's, which may for example arise due to single women sorting into more stable occupations (Bertrand, 2011). When solving the model, I discretize the income processes using the Rouwenhorst method (Rouwenhorst, 1995).

Finally, I set the mean of the persistent part of the stochastic income component during recessions (μ_z^{rec}) to -0.06. Thereby, I ensure that the correlation between stock market and human capital returns is positive but does not exceed estimates from previous literature, in particular Huggett and Kaplan (2016).¹⁴

¹³ Details on the estimation strategy can be found in Appendix C.1. When estimating the stochastic part of the income process, I drop individuals who report zero income to avoid unrealistically high estimates for

Table 2: Estimation Results – Stochastic Income Process

Parameter	Men	Women	Men	Women
	Singles		Couples	
$ ho_z$	0.9524 (0.0078)	0.9352 (0.0099)	0.9353 (0.0046)	0.9273 (0.0045)
σ_z^2	0.0897 (0.0115)	0.0854 (0.0120)	0.0809 (0.0051)	0.1583 (0.0092)
$\sigma_{ ilde{y}}^2$	0.1693 (0.0342)	0.1552 (0.0224)	0.1412 (0.0109)	0.2851 (0.0177)

Notes: Standard Errors in parentheses obtained with bootstrapping (2000 replications).

Marital Transitions. Marital transitions are defined as the likelihood of getting married (respectively divorced) within the next period conditional on not being married (respectively being married) in the current period. More specifically, I estimate the following logit function, separately for couples and singles:

$$\zeta_{i,j+1} = \frac{exp(\mathbf{x}'_{ij}\boldsymbol{\beta}^s)}{1 + exp(\mathbf{x}'_{ij}\boldsymbol{\beta}^s)}$$

where $\zeta_{i,j+1}$ denotes the probability for household i in period j of being married (respectively divorced) next period. As explanatory variables (\boldsymbol{x}) , I include age, education, and a dummy for waves after 1997 to account for the switch from annual to biannual frequency in the PSID. For couples, age refers to the household head. Table 12 in Appendix C.3 reports the corresponding regression coefficients $(\boldsymbol{\beta}^s)$.

The likelihood of both marriage and divorce declines over the life-cycle. At any given age, single women are less likely than single men to get married. The probability of marriage is increasing in education whereas divorce becomes less likely if both spouses have more than 12 years of schooling. Finally, I estimate the matching of spouses in terms of income and

the income volatility, in particular among married women.

¹⁴ See Appendix C.1 for details on the definition and estimation of human capital returns and their correlation to the risky asset.

education (summarized by the term Π) non-parametrically from the PSID.

Out-of-Pocket Medical Expenditures. I borrow the parameters describing medical expenditures by age and gender from Borella et al. (2020). The authors estimate deterministic out-of-pocket medical expenditures profiles with data from the HRS separately for men and women. They estimate higher medical expenditures for men at the start of retirement but a steeper gradient for women, especially after age 76.

Survival Probabilities. I take gender-specific death probabilities from the Life Tables of the U.S. Social Security Administration.¹⁵ The death probability at age j is defined as the probability to die within the next year conditional on having survived up to age j. I compute the inverse of those probabilities and work with average values between the years 1990, 2000, and 2010, corresponding to the sample period of my study. For couples, if the husband dies, the surviving wife keeps 60% of the household's assets, whereas a surviving husband keeps 70% of the household's assets to account for sharply increasing medical expenses in the year prior to death, as well as for bequests to non-spousal heirs.¹⁶

Asset Returns. The annual return rate of the risk-free asset is 2%, taken from Catherine (2022). During booms, the return of the risky asset is drawn from a normal distribution with mean $\mu_r^{\text{boom}} = 11.5\%$ and variance $\sigma_r^2 = (0.1758)^2$. During recessions, the mean return to the risky asset is $\mu_r^{\text{rec}} = -24.5\%$. A recession occurs each period with probability $p_{\text{rec}} = 14.6\%$. Hence, in expectations, the equity premium is 5%. The values for p_{rec} , μ_r^{boom} , and μ_r^{rec} are again taken from Catherine (2022) whereas σ_r^2 reflects the variance of the annual total return index of the S&P 500 from 1989 until 2016.

Pension Payments. Pension payments are flat and assumed to be 60% of the medium persistent income realization at age 65. To ensure that on aggregate pensions are correlated with

¹⁵ All tables are available under this link.

¹⁶ I choose these values because Jones, De Nardi, French, McGee, and Rodgers (2020) document that households who experienced the death of one spouse have around 30% lower wealth than couples who did not experience a death, and that surviving single men are on average wealthier than surviving single women.

lifetime income, I assume that individuals in the lowest productivity state at 65 receive 60% of the income that corresponds to the lowest transitory realization of the medium persistent state, singles with a medium productivity receive a pension corresponding to the medium transitory realization of the medium persistent state and so forth. Couples receive a common pension that is 1.7 times higher than that of single men.

Equivalence Scales. To calibrate the equivalence scales η , I compute the average number of household members by age and family type from the PSID and then apply the OECD equivalence scale: I assign a weight of 1 to the first adult household member, a weight of 0.7 to all other adult members, and a weight of 0.5 to each child.

Initial Conditions. The initial distribution over asset holdings in the model is chosen such that it mimics the distribution of net worth across individuals at age 30 in the SCF. Similarly, I set the fraction of high- and low- educated individuals by gender to be the average share of individuals with more or less than 12 years of schooling in the PSID. The initial distribution of couples and singles is set equal to PSID data for individuals at age 30.

4.2 Second Stage Calibration

I borrow the bequest parameters from Cooper and Zhu (2016) which results in L=0.128 and $\omega=0.73$. Next, to impose structure on the age-profile in the stock market participation costs (S_j^F) , I assume that the highest participation cost (i.e., at age 65) is \$300 above the cost for young households. Moreover, the costs start to increase linearly from age 45 onward. These restrictions leave me with one participation cost parameter to calibrate internally (S_{young}^F) . Taking the parameters from the first stage as given, I then calibrate the structural parameters $\Theta = \{\beta, \gamma, S_{\text{young}}^F\}$ using the Simulated Method of Moments. The exercise is to find $\hat{\Theta}$ that

solves the following optimization problem:¹⁷

$$\mathcal{L} = \min_{\Theta} \left(\frac{M^s(\Theta) - M^d}{M^d} \right) W \left(\frac{M^s(\Theta) - M^d}{M^d} \right)'$$

where W represents a weighing matrix, M^d moments derived from the data and $M^s(\Theta)$ their theoretical counterparts derived from model simulations. I take the relative deviation of simulated moments from their data targets as input in the objective function to account for different units (%-points vs. \$ values) across empirical moments.

Parameter Identification & Choice of Moments. I exploit heterogeneity in wealth levels to identify the discount factor β . Once households cross the threshold of stock market participation, the participation cost becomes irrelevant for their decision on how much to invest in the risky asset. Taking this discrepancy into account, I identify the coefficient of risk aversion γ by exploiting heterogeneity in the portfolio share conditional on participating. The stock market participation cost S_{young}^F serves as the target to match participation rates. I target the life-cycle profiles of single men and single women, resulting in 216 moments (36 years \times 3 variables \times 2 HH types), with only three parameters.

The Weighting Matrix W. I first calibrate the second-stage parameters by using a slightly modified identity matrix $(W = \mathcal{I})$. Given the paper's focus on equity share, I place less weight (30%) on asset profiles than on participation rates and conditional risky shares. In a second run, I use the inverse of the variances of my moment conditions as a (diagonal) weighting matrix to assign a lower weight to less precisely estimated data moments $(W = \frac{1}{\mathcal{V}})$. This approach follows Cooper and Zhu (2016) and is in contrast to papers that use the standard variance-covariance matrix (e.g. Cagetti (2003) or Alan (2006)). In the current set-up, different moments are based on different sample sizes: while participation rates and wealth levels include all observations, the conditional risky share only includes stock market participants.

¹⁷ Given the computational complexity of the framework, I can only solve the model for a limited number of iterations. See Appendix D.1 for further details.

Hence, I could only estimate covariances for the restricted sample of stockholders which is not necessarily more informative than the diagonal matrix.

5 Quantitative Results

5.1 2nd Stage Parameters

Table 3 reports the calibrated second-stage parameters. The parameter values across the two specifications are very similar. The calibration with the modified identity matrix ($W = \mathcal{I}$) finds an annual stock market participation cost of \$288 for young households which increases to \$588 at age 65. With regard to the coefficient of risk aversion, my estimates suggest $\gamma = 5.19$ which is in line with previous papers of portfolio choice that allow for a small dependence between stock returns and labor income shocks. For example, Shen (2023) estimates a degree of risk aversion of $\gamma = 5.6$. Catherine (2022) finds a CRRA coefficient of $\gamma = 6$ and an annual stock market participation cost of \$250 which is very close to my results. In addition, my value for β (0.927) is well within the range of previous studies. Cooper and Zhu (2016) estimate a discount factor of 0.869, Fagereng, Gottlieb, and Guiso (2017) of 0.77, Catherine (2022) of 0.96, and Shen (2023) of 0.98 for stockholders and 0.92 for non-stockholders.

Table 3: 2nd Stage Parameters

W	β	γ	S_{young}^{F}	S_{old}^F
\mathcal{I}	0.927	5.19	\$288	\$588
$\frac{1}{\mathcal{V}}$	0.918	5.31	\$228	\$528

Notes: Table 3 lists the values for internally calibrated model parameters. W denotes the weighting matrix, as explained in Section 4.2.

5.2 Model Fit

Life-Cycle Profiles of Household Finances. Figure 3 shows that the model matches well the life-cycle profiles of equity shares, participation rates, and conditional risky shares for both single men and single women. Importantly, the model is able to capture the gender

investment gap without introducing preference heterogeneity across households. In addition, the model closely replicates the evolution of net worth for single men and single women until age 50 (Figure 4). However, it slightly undershoots the asset accumulation of single men during older ages. Appendix D.2 further discusses the model fit for couple households.

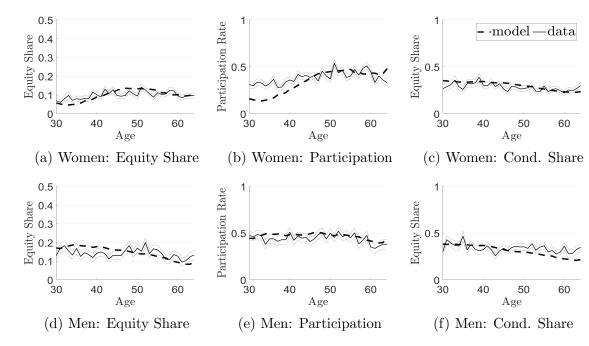


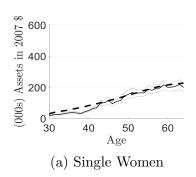
Figure 3: Model Fit of Investment Patterns (Singles)

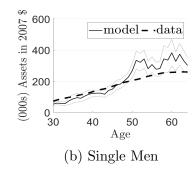
Notes: Figure 3 plots the model fit of equity shares, participation rates, and conditional risky shares for single women and single men. The solid lines show the data (including 95% confidence bands, as plotted in Figure 1) whereas the dashed lines display the simulated life-cycle profiles generated from the model.

Simulated Regressions. To compare the reduced form regressions from Section 2.3 with the model, Table 4 replicates the same regressions on data generated from model simulations. All of these coefficients are untargeted in the calibration exercise.

The model over-predicts the effect of gender on the equity share (Columns (1) and (2) in Table 4), meaning that the absolute values for the coefficient "single woman" and its interaction term with age are larger than in the SCF. However, the simulated data replicates the negative, but increasing marginal effect ("ME") of being a woman on the equity share over the life-cycle. Thus, reduced form regressions that control for household heterogeneity fail to fully explain the gender investment gap, in particular among young households, even if the underlying

Figure 4: Model Fit of Net Worth (Singles)





Notes: Figure 4 plots the model fit of asset accumulation (expressed as net worth) for single women and single men. The solid lines show the data (including 95% confidence bands, as plotted in Figure 1) whereas the dashed lines display the simulated life-cycle profiles generated from the model. Data lines are smoothed using a three-point moving average.

data generating process assumes homogeneous preferences across men and women.

Columns (3) and (4) report the estimated gender effect on stock market participation rates. In line with the data, the model predicts the marginal effect of being a woman to be negative and increasing in age. In both data and model, the marginal effect of being a woman on the participation rate accounts for the majority of the overall marginal effect on the equity share. When considering the conditional risky share (Columns (5) and (6)), the model produces a negative baseline effect of being a woman (in line with the data, albeit non significant), and a negative interaction term (opposed to a positive one in the data). Hence, even though the model matches the marginal effect of being a woman on the conditional equity for young households, it predicts, in contrast to the data, an increasing trend over the life-cycle.

As in the SCF, the coefficient for income is positive across all specifications on model simulated data. The model also replicates the positive coefficient for safe assets with regard to the equity share and participation rate, and a negative coefficient in the specification for the conditional risky share. All else equal, higher net worth helps households to pay the stock market participation cost. However, conditional on participating, the optimal risky share is slightly decreasing in household wealth, explaining the negative coefficient for safe assets in Column (5).

With model simulated data, the coefficient for age is positive, that of its squared term

negative, and that of its cubic term positive which is in contrast to the SCF for participation rates and equity shares. Finally, the coefficient for high education is positive throughout all six specifications. In the model, education increases deterministic income, making highly educated households more willing (and able) to participate in risky asset markets.

6 Understanding the Mechanisms

As Table 4 shows, reduced form regressions that control for household heterogeneity fail to fully explain the gender investment gap, even if the underlying data generating process assumes homogeneous preference parameters across men and women. To better understand what drives gender heterogeneity in equity shares, this section analyzes gender specific model elements more carefully and explains how they affect households' investment choices.

6.1 Decomposing the Gender Investment Gap

First, I decompose the gender gaps in equity shares and wealth levels along the dimensions of gender heterogeneity in the model, that is along the deterministic part of the income process and its individual components, the stochastic part of the income process, marital transition probabilities, the expected characteristics of the partner in the event of marriage (the "marriage market": Π), the distribution of individuals across education levels, initial wealth holdings, the average number of household members (captured by the equivalence scale η), as well as medical expenses and survival probabilities during retirement. In all cases, I replace the female value with that of men and study the resulting gender gaps in asset holdings and equity shares. Table 5 displays the results. The column "Model" reports the gender gap in the respective counterfactual whereas the column "% explained" indicates how much of the baseline gap can be explained through that particular channel.

Decomposing the Gap in Wealth Levels. The upper panel of Table 5 shows that differences in the deterministic part of income, stochastic part of income, and household sizes explain the largest fraction of the wealth gap between single men and single women.

Table 4: Regression Coefficients & Marginal Effects – Data vs. Model Simulations

	(1) Equity	(2) Share	(3) Participa	(4) tion Rate	(5) Condition	(6) nal Share
	Model	Data	Model	Data	Model	Data
single woman	-0.5603° (0.0323)	-0.1665 ^{\disp} (0.0121)	-0.4855° (0.0349)	-0.1345 ^{\disp} (0.0116)	-0.0932° (0.0103)	-0.0196 (0.0170)
single woman*age	0.0099^{\diamond} (0.0007)	0.0026^{\diamond} (0.0002)	0.0083^{\diamond} (0.0007)	0.0025^{\diamond} (0.0002)	0.0017^{\diamond} (0.0002)	-0.0008^{\diamond} (0.0004)
age	0.2101^{\diamond} (0.0255)	-0.0482^{\diamond} (0.0166)	0.0035 (0.0283)	-0.0912^{\diamond} (0.0148)	0.1109^{\diamond} (0.0076)	0.0305^{\diamond} (0.0117)
$age^2 * 100$	-0.4798^{\diamond} (0.0547)	0.1185^{\diamond} (0.0357)	-0.0468° (0.0610)	0.2113^{\diamond} (0.0327)	-0.2530° (0.0162)	-0.0587° (0.0242)
$age^3 * 10000$	0.3389° (0.0381)	-0.0965° (0.0251)	0.0453° (0.0428)	-0.1604^{\diamond} (0.0232)	0.1821^{\diamond} (0.0112)	0.0391° (0.0162)
high education	0.0342^{\diamond} (0.0069)	0.2449° (0.0018)	0.0224° (0.0079)	0.2571° (0.0018)	0.0287^{\diamond} (0.0021)	0.0542^{\diamond} (0.0032)
no. of HH members		-0.0557^{\diamond} (0.0020)		-0.0405^{\diamond} (0.0007)		-0.0235^{\diamond} (0.0012)
non-asset income	0.0495^{\diamond} (0.0039)	0.0326^{\diamond} (0.0007)	0.0563^{\diamond} (0.0045)	0.0292^{\diamond} (0.0004)	0.0064° (0.0011)	0.0055^{\diamond} (0.0006)
safe assets	0.1498^{\diamond} (0.0041)	0.0217^{\diamond} (0.0012)	0.2174^{\diamond} (0.0042)	0.0147^{\diamond} (0.0003)	-0.0604° (0.0012)	-0.0380° (0.0006)
constant	-5.1159° (0.3905)	-0.1669 (0.2403)	-2.3283^{\diamond} (0.4246)	1.1309° (0.2165)	-0.5337^{\diamond} (0.1169)	0.0902 (0.1873)
Observations Year FE	10,239 No	10,239 Yes	10,239 No	10,239 Yes	4,166 No	4,285 Yes
ME at age 30	-0.2620° (0.0137)	-0.0888 ^{\(\frac{1}{2}\)}}	-0.2359 ^{\(\frac{1}{2}\)}}	-0.0583 ^{\(\frac{1}{2}\)} (0.0048)}	-0.0432 ^{\disp} (0.0045)	-0.0440° (0.0064)
ME at mean age (47)	-0.0930^{\diamond} (0.0069)	-0.0438° (0.0034)	-0.0945° (0.0077)	-0.0142° (0.0018)	-0.0148° (0.0021)	-0.0592^{\diamond} (0.0026)
ME at age 65	0.0861^{\diamond} (0.0130)	0.0019 (0.0032)	0.0553^{\diamond} (0.0150)	0.0307^{\diamond} (0.0040)	0.0152^{\diamond} (0.0038)	-0.0725° (0.0072)

Notes: Estimations are based on linear regressions on the sample of individuals who live in households with no spouse present. Columns "Model" are model simulations, whereas columns "Data" refer to data from the SCF waves 1989 until 2016. Equity Share = Unconditional risky share. Participation Rate = Stock market participation rate. Conditional Share = Conditional risky share. single woman is a dummy indicating that the household head is a woman. high education is a dummy equal to one if the household head has more than 12 years of education. safe assets refers to all net worth that is not invested in risky assets. "ME" indicates the marginal effect of being a woman at the respective age. Robust standard errors in parentheses, \diamond p<0.05.

Overall, heterogeneity in the deterministic part of income explains 40% of the "gender wealth gap". However, this result masks substantial heterogeneity among the individual components of deterministic income. Only replacing the constant \bar{y} of single women with its male counterpart reverses the gender gap in asset holdings. In contrast, adjusting only the age-specific component ξ or – to a lesser extent – the education premium θ further widens the gap. When estimating the deterministic income component on PSID data (see Table 11 in Appendix C.2), I find a negative coefficient of being a single woman, as opposed to a positive interaction term of being a single woman with age and education. Consequently, when replacing the female constant \bar{y} with that of single men, it will be multiplied by the larger female age and education specific interaction term, resulting in the reversed gender wealth gap. In contrast, adjusting the age-specific term ξ not only affects the slope of single women's deterministic income but also reduces their lifetime earnings and asset holdings.

Next, I perform two additional exercises to isolate how the level vs. slope of deterministic income affect the gender wealth gap. First, to analyze the importance of gender heterogeneity in the slope of deterministic income, I again change the age-component ξ of single women to their male counterpart but readjust the female constant such that – on average – single women have the same deterministic income as in the baseline. Hence, I fix the level of female deterministic income but adjust the slope to be equal to that of single men. Second, to analyze the importance of gender heterogeneity in the level of deterministic income, I increase single women's deterministic income at each age by the average difference between men and women. As a result, single women will have on average the same deterministic income as single men while their slope remains as in the baseline. As Table 5 shows, adjusting the slope accounts for 19% of the gap, whereas adjusting the level accounts for 33%. That is, level differences in deterministic income are a more important determinant of gender differences in net worth than heterogeneity in its slope.

In addition, the income process of single women exhibits a smaller overall variance than that of single men (see Table 2). Therefore, assigning single women the stochastic part of the male income process increases female precautionary savings. This channel in isolation explains 41% of the overall wealth gap. Gender differences in household sizes further explain 43% because larger female household sizes (mainly through the presence of children) act as a consumption commitment and lower single women's ability to save.

The remaining channels are quantitatively less important for explaining gender heterogeneity in asset holdings. Increasing single women's marriage probability to that of single men reduces their savings motive as they become more likely to end up in the financially beneficial state of marriage. Assigning single women the male partner's characteristics in the event of marriage (marriage market) in contrast lowers the gender wealth gap because single women expect their prospective partners to be less wealthy and educated, lowering the financial returns to marriage.

Assigning single women the male medical expenses, survival probability, and male fraction of highly educated individuals does not substantially alter the gender wealth gap. Simulating the model under the assumption that both single men and single women start from the same (male) wealth level reduces the wealth gap early in life but has little effect on asset holdings during old age.

Decomposing the Gap in Equity Shares. Similar to asset holdings, differences in deterministic income and household sizes explain the largest fraction of the gender gap in equity shares (see lower panel of Table 5). In contrast, heterogeneity in stochastic income contributes to widening the gap.

Assigning single women the male deterministic income explains around 60% of the gender investment gap. Further decomposing this mechanism into the contribution of slope vs. level (as explained above) reveals that gender heterogeneity in the slope of deterministic income accounts for 19% of the gap, whereas level differences account for 40%.

On average, single men's deterministic income is higher than that of single women. As

Table 5: Decomposition Results

Gap in Asset Holdings in (000s) 2007 \$	Model	% explained	Data
Baseline	48.18		87.52^{a}
Male deterministic income	29.31	39.16%	
only: constant (\bar{y})	-100.76	309.11%	
age component (ξ)	90.87	-88.59%	
education premium (θ)	57.42	-19.17%	
Male determ. income: slope effect	39.17	18.71%	
Male determ. income: level effect	32.14	33.29%	
Male stochastic income	28.57	40.71%	
Male HH size	27.35	43.25%	
Male marriage probability	53.48	-10.99%	
Male marriage market	42.43	11.95%	
Male education distribution	46.11	4.31%	
Male medical expenses	45.99	4.56%	
Male survival probability	47.59	1.23%	
Male initial wealth	35.62	26.08%	
Gap in Equity Share in $\%$ - points	Model	% explained	Data
Baseline	4.45		4.24
Male deterministic income	1.89	57.67%	
only: constant (\bar{y})	-8.06	280.91%	
age component (ξ)	9.99	-124.32%	
education premium (θ)	5.57	-24.96%	
Male determ. income: slope effect	3.64	18.31%	
Male determ. income: level effect	2.68	39.73%	
Male stochastic income	7.44	-67.08%	
Male HH size	-1.56	134.99%	
Male marriage probability	4.63	-3.32%	
Male marriage market	3.09	30.63%	
Male education distribution	4.63	-3.98%	
Male medical expenses	4.47	-0.25%	
Male survival probability	4.80	-7.65%	
Male initial wealth	2.28	48.83%	

Notes: Table 5 shows the results of the decomposition exercise. The column "Model" reports the average gender gap in the respective counterfactual. The column "% explained" indicates how much of the baseline gap can be explained through that channel. All values refer to averages over the life-cycle.

^a The lower wealth gap in the model compared to the data mainly arises from the model's inability to explain the fast asset accumulation of single men beyond age 50 (see Figure 4). However, when replicating the decomposition exercise on the sample of households below 50 (i.e., for which the model matches the data better), the relative importance of the respective channels hardly changes.

a result, when adjusting the female level to its male counterpart, single women's lifetime income increases, making them more likely to invest in risky assets. However, as visible from Figure 2b, the life-cycle path of single men's deterministic income is more 'front-loaded', in that single women start from a lower level but catch up to men as they age. Consequently, when equating the slope of female deterministic income to that of single men, the equity share of single women increases especially early in life, as they now start from a higher level. Participating in the stock market during young ages has the advantage to earn higher returns in expectation, thereby accumulating more wealth, and, as a result, becoming more likely to also participate when old. Thus, despite single women having the same lifetime income as in the baseline, equating their slope to that of single men increases the average female equity share. Hence, it is not only gender heterogeneity in the level of deterministic income per se that matters for explaining the gender investment gap, but also its distribution over the life-cycle.

Changing the constant \bar{y} of single women to its male value scales the entire female deterministic income path upward. That is, single women start from a higher level and their deterministic income increases faster than that of single men (due to the positive interaction term of being a single woman with age, see Table 11). As a result, the gender investment gap reverses quite substantially. In contrast, adjusting the age component ξ widens the gender gap in equity shares. Single women start from a lower level and, at the same time, their deterministic income grows slower than before, reducing female lifetime income.

Moreover, eliminating heterogeneity in household sizes reverses the gender investment gap. Reducing female household sizes to that of single men decreases female consumption needs both contemporaneously and in future periods. As a result, single women are able to accumulate more wealth which increases their likelihood of investing in the risky asset. In addition, lower future consumption needs make households less vulnerable to shocks, further

¹⁸ Higher deterministic income may affect the equity share by making households more likely to cross the participation threshold and by increasing their risky share, conditional on participating. See Section 6.2 for a more detailed discussion on the relative importance of both channels.

increasing single women's willingness to take risks in financial markets.

When single women face the same stochastic income as single men, the gender gap in equity shares increases by 67%. Since the income process of single men has a higher overall variance than that of single women (see Table 2), assigning single women male stochastic income component lowers their willingness to take financial risk, despite them accumulating more wealth on average. Consequently, adjusting overall income (i.e., both the deterministic and stochastic component) of single women to that of single men has a smaller impact on the gender investment gap than changing each component individually, as the two elements partly offset each other. Note, however, that I control for overall income in the data (Table 1), alluding to why controlling for income does not close (or, at least, does not narrow more strongly) the empirical gender investment gap, despite heterogeneity in income being an important driver of differences in equity shares between single men and single women.

Altering the marriage market explains around 30% of the gender investment gap which is mainly driven by higher female asset holdings, as single women expect their partner to be less wealthy and educated. Finally, when single women start from the same wealth level as single men, the gender investment gap substantially declines among young households. This result arises from wealthier young single women being more likely to cross the participation threshold, as opposed to them allocating a larger share of their net worth to the risky asset. Hence, already at age 30, the wealth gap between single women and single men is sufficiently large to prevent single women from participating in risky asset markets.

6.2 Composition vs. Policy Effect

In the model, the equity share for individual s, α_s , is determined by the policy function $\phi(X_s)$ which maps the individual's state variables X_s into the optimal equity share. In turn, aggregate portfolio allocations are determined by individual policy functions and the distribution of individuals across the state space: $\frac{1}{S} \sum_{s=1}^{S} \alpha_s = \frac{1}{S} \sum_{s=1}^{S} \phi(X_s)$.

Thus, gender differences in aggregate investment patterns can arise either because the distribution of individuals across the state space differs ("composition effect") or because of gender heterogeneity in policy functions at any given point in the state space ("policy effect"). The objective of this section is to quantify the relative importance of each effect on the gender investment gap along the life-cycle.

To do so, I decompose average investment differences between single men (m) and single women (f) in the model at every age j according to:

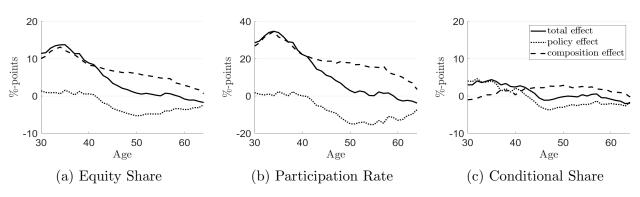
$$\frac{1}{F} \sum_{f=1}^{F} \phi(X_f; f) - \frac{1}{M} \sum_{m=1}^{M} \phi(X_m; m) \approx \underbrace{\left[\frac{1}{F} \sum_{f=1}^{F} \phi(X_f; f) - \frac{1}{F} \sum_{f=1}^{F} \phi(X_f; m)\right]}_{\text{Policy Effect}} + \underbrace{\left[\frac{1}{F} \sum_{f=1}^{F} \phi(X_f; m) - \frac{1}{M} \sum_{m=1}^{M} \phi(X_m; m)\right]}_{\text{Composition Effect}}$$

The first difference on the right-hand side is the policy effect (i.e., fixing the vector of state variables and letting the policy functions for the equity share differ) and the second difference is the composition effect (i.e., fixing the policy functions and letting the vector of state variables differ).¹⁹ Figure 5a plots the importance of each effect over the life-cycle, that is how many percentage points of gender differences in equity shares can be explained by either effect. Figures 5b and 5c repeat the same exercise separately for the extensive margin (participation rates) and intensive margin (conditional risky shares).

The composition effect explains the majority of gender differences in unconditional equity shares early in the life-cycle. That is, most of the gender investment gap among young households arises from differences in the sample composition. Until age 40, heterogeneity in policy functions explains around 10% of the overall gap. Beyond that age, the policy effect has a negative impact on gender differences in equity shares, meaning that single women

 $^{^{19}}$ I thank an anonymous referee for suggesting this illustrative way of separating the composition from the policy effect.

Figure 5: Composition vs. Policy Effect – Aggregate



Notes: Figure 5 decomposes the aggregate gender gaps in (unconditional) equity shares, participation rates, and conditional risky shares into a composition and policy effect along the life-cycle. The composition effect (dashed line) shows what part of the overall gap can be explained through gender differences in the sample composition whereas the policy effect (dotted line) shows what part of the gap can be explained by differences in policy functions, conditional on state variables.

take *more* financial risk than single men. When further separating the extensive from the intensive margin, I find that compositional differences primarily affect participation rates. That is, low female wealth levels early in life prevent single women from entering the stock market. In contrast, the gender gap in conditional risky shares among young households is mostly explained by heterogeneity in policy functions (Figure 5c).

However, as discussed in Section 6.1, individual model elements affect the gender investment gap in opposite directions. Thus, Figure 5 may mask substantial heterogeneity about the relative importance of these individual channels. To analyze such heterogeneity, Figure 6 further decomposes the policy effect into its contribution arising from deterministic income, household sizes, and stochastic income.²⁰ The solid lines denote the total gender investment gap, the dashed lines the composition effect, the dash-dotted lines indicate how much of the policy effect can be accounted for by the respective channel, and the dotted lines illustrate the importance of all remaining factors (as listed in Table 5) for the policy effect.²¹

To do that, I decompose the policy effect according to: $\frac{1}{F}\sum_{f=1}^{F}\phi(X_f;f)-\frac{1}{F}\sum_{f=1}^{F}\phi(X_f;m)\approx \left[\frac{1}{F}\sum_{f=1}^{F}\phi(X_f;f)-\frac{1}{F}\sum_{f=1}^{F}\phi(X_f;cf)\right]+\left[\frac{1}{F}\sum_{f=1}^{F}\phi(X_f;cf)-\frac{1}{F}\sum_{f=1}^{F}\phi(X_f;m)\right]$, where cf denotes the respective counterfactual model simulation. Accordingly, the first term on the right hand side is the part of the policy effect that can be explained by the respective counterfactual(s) and the second term is the part that can be explained by all remaining factors.

²¹ Figures 15 and 16 in Appendix D.3 document the corresponding results for participation rates and conditional risky shares.

In Figure 6a, the dash-dotted line (i.e., the part of the policy effect can be explained by deterministic income) is slightly above the dotted line (i.e., the part of the policy effect can be explained by all other channels), meaning that lower female deterministic income contributes to single women taking less financial risk (conditional on state variables). When separately considering the extensive and intensive margin (see Figures 15 and 16 in Appendix D.3), I find that lower deterministic income affects female policy functions both with regard to the participation decision and, to a larger extent, conditional risky share.

How does deterministic income affect individuals' policy functions? When deciding on the optimal equity share, forward-looking agents take into account both their contemporaneous state variables (e.g. their current level of wealth and income) as well as all future variables. That is, conditional on a certain position in the state space, policy functions differ between single men and single women because of heterogeneity in future outcomes. As long as the risky asset return is only mildly correlated to income shocks (that is, as long as labor income is rather bond than stock-like), a higher human capital endowment (i.e., higher expected discounted earnings) increases households' willingness to take financial risk. Hence, conditional on their level of wealth (and other state variables), it is optimal for single women to invest less in the risky asset because their income is in expectation lower than that of single men (see Figure 2), especially early in the life-cycle.

Moreover, gender heterogeneity in household sizes mainly affects the gender investment gap through its impact on policy functions (Figure 6b). In the model, forward-looking single women understand that they will have higher consumption needs (through larger household sizes) in future periods, making them more vulnerable to financial shocks and decreasing their willingness to invest in the risky asset already in the current period.

Finally, as shown in Figure 6c, gender heterogeneity in stochastic part income lowers the total policy effect. The income process of single women is characterized by a smaller variance than that of single men (Table 2), making single women more willing to take financial risk

(conditional on state variables). The increased willingness to invest in the stock market affects both their decision to participate, as well as their optimal risky share conditional on participating (see Figures 15 and 16).

30 30 30 total effect total effect total effect - composition - composition - composition 20 20 20 ...policy: other factorspolicy: other factorspolicy: other factors %-points %-points policy: det. income policy: HH sizes policy: stoch. income 0 0 0 -10 ^{_} 30 -10 ^{_} 30 -10 ^{_} 30 50 60 50 60 50 60 Age Age Age (c) Stochastic Income (b) Household Sizes (a) Deterministic Income

Figure 6: Further Decomposition of Policy Effect

Notes: Figure 6 decomposes the aggregate gender gaps in (unconditional) equity shares, participation rates, and conditional risky shares into a composition and policy effect along the life-cycle. The composition effect (dashed line) shows what part of the overall gap can be explained through gender differences in the sample composition whereas the policy effect (dotted line) shows what part of the gap can be explained by differences in policy functions, conditional on state variables.

Thus, on aggregate it seems that heterogeneity in the sample composition (that is, in contemporaneous characteristics) is most important to explain the gender investment gap. However, further analysis reveals that gender heterogeneity in the main determinants of the gap – deterministic income, household sizes, and stochastic income – all contribute to policy functions for the risky share to differ across single men and single women, albeit in different directions. Conditional on their position in the state space, policy functions across households differ because of heterogeneity in future outcomes, something one cannot as easily control for in reduced form regressions.

6.3 Additional Evidence

The decomposition exercise in Section 6.1 revealed that heterogeneity in deterministic income and household sizes are important determinants of the gender investment gap. Moreover, as shown in Section 6.2, both contemporaneous and future outcomes of both variables matter for current period investment choices.

The purpose of this section is to provide further evidence of these channels in the data, as

they cannot be easily controlled for in reduced form regressions. First, I show that controlling for proxies of deterministic income (as opposed to only overall income) helps to reduce the empirical gender investment gap. Second, I provide direct survey evidence on singles' perceptions about future household sizes and (overall) income.

Controlling for Deterministic Income Proxies. According to the structural model, controlling for observable characteristics that proxy for 'deterministic income' should narrow empirical gender differences in investment choices. In fact, including occupation and industry fixed effects (that arguably contain information about the deterministic part of income) in the regressions from Table 1 shrinks the baseline gender effect from 17%-points to 12%-points (Columns (3) and (4) in Table 1). In addition, the estimated age gradient of being a single woman becomes smaller. Thus, including occupation and industry fixed effects helps to reduce the unexplained part of the investment gap in particular among young households for whom differences in deterministic income are largest (see Figure 2).

Direct Survey Evidence. Neither the PSID nor SCF contains information on individuals' perceptions about future income or household sizes. Therefore, I complement the analysis with data from the New York Fed Survey of Consumer Expectations (SCE).²² The SCE asks respondents about their expected annual earnings in four months and the expected number of individuals living in the same household one year from the time of the interview. However, note that in the SCE, annual earnings refer to overall income, that is both deterministic and stochastic income in the model. Thus, one should not regard this exercise as a direct mapping from model to data but rather as suggestive evidence whether women predict their income to be lower than that of single men in future periods. In particular, conditional on the same current overall income, single women should be on average more likely to have a positive transitory income shock (because their deterministic income is lower) and thus, more likely to predict their earnings to be below those of single men in the next period.

²² See Appendix A.3 for details about this data set and variable construction.

I regress expected annual earnings of single households on a gender dummy while controlling for current earnings, education, age, year- and region-fixed effects (Column (1) in Table 6). In Column (2), I additionally control for the inverse hyperbolic sine of financial wealth. In line with the proposed model mechanism, single women expect their future earnings to be 9-16% lower than that of single men, depending on the specific set of included control variables.²³ When splitting the sample by age (Columns (3) and (4)), I find that gender differences in income expectations are larger among younger singles, when gender differences in deterministic income are largest (Figure 2).

Table 6: Expected Earnings of Single Households – SCE Data

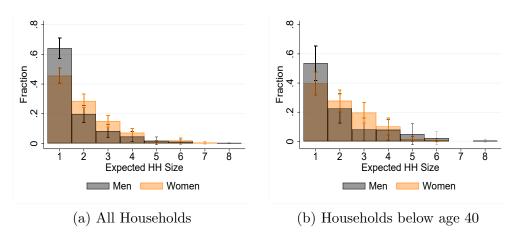
	(1) log(exp. earnings)	(2) log(exp. earnings)	$\begin{array}{c} (3) \\ \log(\text{exp. earnings}) \\ \text{Age} \leq 45 \end{array}$	$\begin{array}{c} (4) \\ \log(\text{exp. earnings}) \\ \text{Age} > 45 \end{array}$
single woman	-0.1619 ^{\disp} (0.0376)	-0.0922° (0.0464)	-0.2394° (0.0548)	-0.0915 ^{\displaystyle} (0.0445)
$\log(\text{current earnings})$	0.6556^{\diamond} (0.0502)	0.5792° (0.0670)	0.5712° (0.0648)	0.7927° (0.0550)
high education	0.2617° (0.0365)	0.2132° (0.0481)	0.3591° (0.0524)	0.1429° (0.0382)
1. age > 40	-0.0207 (0.0421)	-0.0186 (0.0460)		
financial wealth		0.0246° (0.0095)		
constant	3.5953° (0.5231)	4.2170° (0.6941)	4.4481° (0.6874)	2.1708° (0.5859)
Observations	3,009	1,697	1,774	1,235
Year FE Region FE	Yes Yes	Yes Yes	Yes Yes	Yes Yes

Notes: Estimations are based on linear regressions on the sample of individuals who live in households with no spouse present. Data is from the SCE waves 2014 until 2019. $single\ woman$ is a dummy indicating that the household head is a woman. $high\ education$ is a dummy equal to one if the household head has more than 12 years of schooling. Robust standard errors in parentheses, \diamond p<0.05.

Furthermore, Figure 7a plots the distribution of expected household sizes for all single house-

²³ The negative coefficient for being a single woman does not mean that women necessarily expect their income to decrease which could be at odds with their steep income slope early in life (Figure 2). The negative coefficient rather states that they expect to earn less *relative to single men*.

Figure 7: Expected Household Sizes of Singles – SCE Data



Notes: Figure 7 plots the histogram of expected household sizes (= expected number of household members) for single households. Figure 7a plots the distribution for the entire sample, whereas Figure 7b restricts the sample to households below age 40. Data is from the waves 2014 until 2019 of the Survey of Consumer Expectations (SCE).

holds whereas Figure 7b restricts the sample to households below age 40. In both cases, single women assign a lower probability to living alone than single men. On the other hand, they are more likely to expect to live with one or more additional household members who are not prospective spouses. Note that these differences largely reflect heterogeneity in the current number of household members. Hence, Figure 7 rather ensures that singles (correctly) predict household sizes to be persistent. Again, this finding aligns with the model where single women have, conditional on age, both larger current and future household sizes.

7 Robustness Checks & Discussion of Assumptions

In this section, I perform several robustness checks and discuss certain assumptions of the structural framework. First, I revisit the presence of child support and spousal maintenance payments. Next, I test the sensitivity of the model results with regard to potential gender heterogeneity in bequests. Finally, I show that my results are robust to variations in exogenously set parameters.

Alimony Payments and Child Support. In the US, official regulations determine the amount of alimony payments and child support following a divorce.²⁴ Typically, the non
24 Spousal and child support in the U.S. are governed by state laws. A comprehensive overview of individual

custodial parent (or, in case of joint custody, the partner living primarily with the child) receives regular payments from either their ex-partner or a government agency to economically support the child. Spousal support, in contrast, is more restricted and depends on factors such as the length of the marriage, relative income of spouses, and their future financial prospects. In both cases, these transfers may alter the income path of singles in the form of a redistribution from single men to single women because women are more likely to be granted custody and tend to earn less than their (former) husbands.

Yet, I abstract from introducing these payments explicitly for two reasons. First, it has been shown that compliance with such laws tends to be low (Del Boca and Flinn, 1995, Case, Lin, and McLanahan, 2003). Second, introducing alimony payments and child support requires an additional state variable that keeps track of the individual's marital history. I, however, account for alimony payments and child support empirically by including them in the income measure. Moreover, I test the sensitivity of the model results with regard to the asset allocation upon divorce and solve a counterfactual version in which the wife receives 65% and the husband 35% of the couple's assets following a divorce (instead of the 50-50 splitting rule assumed in the benchmark). In a parsimonious way, one could think of all alimony and child support claims being paid in a lump-sum transfer directly after divorce instead of being spread out across multiple years.

In response, single men hold on aggregate fewer assets, whereas single women are slightly richer than in the baseline framework. Panel I of Table 7 reports that the resulting gender gap in asset holdings shrinks from on average \$48,000 to \$29,000. Consequently, the gender investment gap shrinks as well from 4.45%-points to 3.16%-points. However, when performing the decomposition analysis of Section 6.1 on the model with this modified asset splitting rule, the most important factors contributing to the observed gaps remain gender differences in deterministic income, household sizes, and stochastic income. That is, the main results of the paper are robust to this modification.

regulations can be found here.

Table 7: Robustness Checks

Gender Gap in	Asset Holdings (in 000s \$)	Equity Shares (in %-points)
Baseline	48.18	4.45
Panel I: Alimony & Child Support Modified splitting rule after divorce	28.99	3.16
Panel II: Bequests Variation in bequest parameters Lump-sum transfer at age 55	49.82 50.51	4.63 4.49
Panel III: Exogenous Parameters Higher correlation of income shocks within couples No asset drop after death of spouse Reduced medical expenses for couples Higher pension payments for couples	47.74 48.16 43.06 44.61	4.09 4.68 4.00 4.39

Notes: Table 7 reports the average gender gap in asset holdings and equity shares in the baseline model, as well as in alternative versions: Panel I performs robustness with regard to alimony payments and child support, Panel II with regard to bequests, and Panel III with regard to exogenously set model parameters. "Gender Gap" describes the difference of the respective variable between single men and single women, averaged over working age. The gender gap in asset holdings is expressed in (000s) 2007\$. The gender gap in equity shares is expressed in percentage points.

Bequests. It may be that both bequests given and bequests received differ by gender, which in turn alters expectations about income and wealth outcomes. To test for this possibility in the data, I exploit a module in the SCF that collects information on whether its respondents have ever received an inheritance and if they expect one in the future. Panel I of Table 8 lists the distribution of these (expected) inheritances by family type. Single men and single women do not differ in the likelihood of ever having received an inheritance. However, conditional on having inherited something, men receive on average more.²⁵ Moreover, single women are less likely to expect an inheritance in the future.

Building on this evidence, I perform a robustness check where I introduce a lump-sum transfer to all households at age 55 in the model. Single men receive \$8,199, single women \$6,876, and couples \$15,322. These values reflect the empirical amount of received bequests times

²⁵ For both measures, I restrict the sample to households above 55 years because Bauluz and Meyer (2022) document that most households in the U.S. inherit wealth when they are between 50 and 60 years old. The results remain qualitatively unchanged when considering the entire sample.

Table 8: Distribution of (expected) Bequests by Family Type (Data)

	Couples	Singles	
		Men	Women
Panel I: Bequests received			
% received inheritance (> 55 yrs)	27.28 (3.43)	22.97 (6.99)	22.60 (5.20)
\$ amount received in (000s) (> 55 yrs)	$56.16 \ \scriptscriptstyle{(1.52)}$	35.70 (2.61)	30.43 (1.78)
% expect inheritance	17.05 (1.39)	14.88 (2.83)	10.24 (1.86)
Panel II: Bequests given			
% perceive bequests as important	51.81 (1.84)	52.23 (4.06)	53.39 (3.08)
% expect to give bequest	56.06 (1.85)	51.63 (4.02)	41.75 (3.07)

Notes: Table 8 reports the distribution of (expected) bequests across family types. "% received inheritance $(>55~\rm yrs)$ " indicates the fraction of HHs above age 55 who have received an inheritance, whereas "\$ amount received in $(000s)~(>55~\rm yrs)$ " indicates the average amount of that inheritance. "% expect inheritance" denotes the fraction of households who expect to receive an inheritance in the future. "% perceive bequests as important" is the fraction who considers leaving something behind as important, and "% expect to give bequest" is the fraction who expects to do so. Standard errors are in parentheses. Data is from the Survey of Consumer Finances (SCF), waves 1989-2016.

the probability of having received something (as shown in the first two rows of Panel I in Table 8). In response to introducing these transfers, households accumulate less wealth in the years leading up to age 55 and hold on average more wealth afterwards. However, given that the received amount is quite similar for single men and single women, the gender gap in asset holdings and equity shares hardly changes when compared to the benchmark (see Panel II of Table 7).

Furthermore, the SCF contains information on whether households perceive leaving bequests as important and if they expect to leave a "sizable estate" to others. Panel II of Table 8 shows that around half of all households consider leaving an inheritance as important, regardless of their family type. Hence, the assumption of homogeneous bequest parameters across all household types is supported empirically. In addition, as I model bequests to be a luxury good, the share of bequeathed wealth is increasing in households' asset holdings, and will therefore be on average highest for couples, followed by single men, and then single women. Again, I confirm this pattern in the data: whereas 42% of single women expect to leave

something behind, 52% of single men and 56% of couples do. Finally, Panel II of Table 7 shows that my results are robust to modifying the exact parameter values of the bequest motive from 0.128 to 12.8 (L) and from 0.73 to 73 (ω).

Variation in exogenously set parameters. Panel III of Table 7 compares the gender gap in equity shares and asset holdings of the baseline model to alternative versions in which I test the robustness with regard to exogenously set parameters. I change – one-by-one – the correlation of transitory income shocks within couples from 0.3 to 0.9, I assume that assets remain constant whenever one spouse dies, that couples only pay 80% of medical expenses to account for informal care arrangements across partners, and that pension payments of couples are twice as large as that of single men (instead of 1.7 times). In all cases, the gender investment gap changes little when compared to the baseline framework.

8 Conclusion

This paper studies the gender investment gap through the lens of a structural life-cycle framework. First, I provide empirical evidence that single women are less likely to participate in the stock market than single men and that they allocate a smaller share of their net worth toward risky assets. This gap remains statistically significant in reduced form regressions after controlling for a wide range of observable characteristics that have been shown to affect investment behavior.

A life-cycle model of portfolio choice that restricts preferences to be equal across men and women is able to replicate the empirical gap. Counterfactual simulations reveal that higher male deterministic income and fewer household members are the main determinants for explaining the gender investment gap. Deterministic income matters both because single women earn less on average (a level effect). Additionally, the gender gap in deterministic income is largest early in life, preventing young single women from participating in the stock market. As a result, they earn lower returns in expectations, accumulate less wealth and are

less likely to participate when old (a slope effect). In contrast, gender heterogeneity in the stochastic part of income contributes to widening the gap.

Finally, both contemporaneous and future deterministic income and household sizes affect current-period investment choices. Because labor income is only mildly correlated to stock returns, a higher human capital endowment increases an agent's optimal equity share for a given level of wealth. Similarly, lower household sizes reduce future consumption needs and increase financial risk-taking already in the current period.

Hence, in line with the empirical evidence, reduced form regressions that control for overall income and do not take into account gender heterogeneity in future deterministic income and household sizes fail to fully explain the gender investment gap.

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A Data Appendix

A.1 Comparability of PSID and SCF

Figure 8 plots the life-cycle profiles of stock market participation rates (excluding stocks held through retirement accounts) and net worth by family type in the PSID, as these are measures that are available in both the PSID and SCF. The life-cycle profiles of stock market participation rates without stocks held through retirement accounts in the PSID (Figure 8a) look very similar to those in the SCF (Figure 9b). Most importantly, I can replicate the converging gender investment gap over the life-cycle. When comparing net worth in the PSID (Figure 8b) to the SCF (Figure 1d), I find that wealth levels in the PSID are lower than in the SCF. However, in both datasets, couples and single men have higher net worth than single women, especially as they approach retirement.

Tigure 8. Effe-Cycle Patterns of Household Pinances – PSID

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Figure 8: Life-Cycle Patterns of Household Finances – PSID

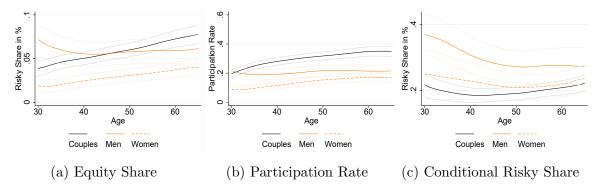
Notes: Figure 8 plots the life-cycle profiles of stock market participation rates and net worth for singles and couples, including 95% confidence intervals. Data is from the waves 1989 until 2017 of the Panel Study of Income Dynamics (PSID). Risky assets are defined as direct stock holdings, excluding stocks held through retirement accounts. Net worth is defined as total assets minus total debt.

A.2 Supplementary Figures

Excluding Retirement Accounts. If single men are more likely to hold retirement accounts than single women, and if individuals, regardless of gender, tend to invest retirement savings riskier than other types of wealth, the gender investment gap could reflect gender heterogeneity in the labor market rather than in investment choices. Figure 9 therefore plots the life-cycle profiles of equity shares, stock market participation rates, and conditional risky

shares based on a tighter definition of risky assets that excludes savings held through retirement accounts. The gender gap in equity shares (Figure 9a) remains statistically significant, alleviating concerns that investment differences across gender are mainly driven through savings that are linked to certain types of jobs.

Figure 9: Life-Cycle Patterns of Household Finances – Excluding Retirement Accounts



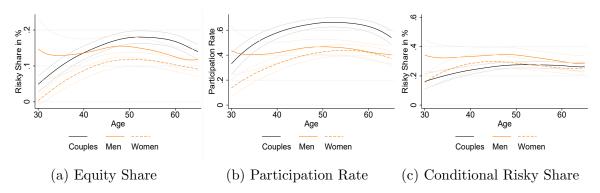
Notes: Figure 9 plots the life-cycle profiles of equity shares, stock market participation rates, and conditional risky shares for singles and couples, including 95% confidence intervals. Data is from the waves 1989 until 2016 of the Survey of Consumer Finances (SCF). Risky assets are defined as direct stock holdings, corporate and foreign bonds, and the fraction of mutual funds that include the former. All figures are smoothed to increase readability.

Cohort Effects. Heterogeneity in the gender investment gap across different ages could be driven by cohort-specific investment behavior (Ameriks and Zeldes, 2004). Therefore, Figure 10 plots the empirical patterns from Figure 1 when restricting the sample to individuals who were born within a relatively short time frame (1945-1960). All three graphs look qualitatively very similar to the baseline, with larger standard errors due to the reduced sample size.

A.3 New York Fed Survey of Consumer Expectations

In Section 6.3, I work with the Labor Market Survey and Household Finance module from the New York Fed Survey of Consumer Expectations (SCE). The SCE is a nationally representative online survey of around 1,300 private households in the U.S. running from 2013 until today. While respondents are interviewed monthly, questions on topical modules are included less frequently. The Labor Market Survey has been collected in March, July, and November since 2014. The Household Finance module has been included each August from 2014 until 2019. I work with all available waves from these two topical modules up until

Figure 10: Life-Cycle Patterns of Household Finances – One Cohort



Notes: Figure 10 plots the life-cycle profiles of equity shares, stock market participation rates, and conditional risky shares for singles and couples, including 95% confidence intervals. Data is from the waves 1989 until 2016 of the Survey of Consumer Finances (SCF) for individuals who are born between 1945-1960. Risky assets are defined as direct stock holdings, corporate and foreign bonds, the fraction of mutual funds that include the former, and the fraction of retirement accounts which is invested in stocks. All figures are smoothed to increase readability.

2019.

I merge both modules to the core data which includes demographic characteristics such as gender and marital status. In the Labor Market module, respondents additionally report their current annual earnings and expected annual earnings in four months, which serves as my dependent variable in Table 6. In the household finance module, respondents indicate the number of household members they expect to live with 12 months from the time of the interview (Figure 7).

In addition, the household finance module contains information about financial wealth, which I use as a control variable in Table 6. Note, however, that households are never asked in the same month about both their expected earnings and financial wealth. Therefore, I extrapolate financial wealth to the months in which households report expected earnings and only include households who answer to both modules. All variables are expressed in June 2014 Dollars.

A.4 Regression Coefficients and Marginal Effects

Table 9: Regression Coefficients & Marginal Effects – Participation Rates of Singles

	(1) SMP	(2) SMP	(3) SMP	(4) SMP
single woman	-0.2868° (0.0103)	-0.1775° (0.0096)	-0.1345° (0.0116)	-0.1084° (0.0117)
single woman * age	0.0049^{\diamond} (0.0002)	0.0031^{\diamond} (0.0002)	0.0025^{\diamond} (0.0002)	0.0018^{\diamond} (0.0002)
age	-0.1362° (0.0140)	-0.0926^{\diamond} (0.0141)	-0.0912° (0.0148)	-0.0920^{\diamond} (0.0222)
age^2*100	0.3205^{\diamond} (0.0305)	0.2228^{\diamond} (0.0308)	0.2113^{\diamond} (0.0327)	0.2113^{\diamond} (0.0492)
$age^3*10000$	-0.2442^{\diamond} (0.0216)	-0.1712^{\diamond} (0.0218)	-0.1604° (0.0232)	-0.1541° (0.0352)
high education		0.2750^{\diamond} (0.0020)	0.2571° (0.0018)	0.1601^{\diamond} (0.0029)
no. of HH members		-0.0417^{\diamond} (0.0007)	-0.0405° (0.0007)	-0.0420^{\diamond} (0.0016)
non-asset income		0.0325^{\diamond} (0.0005)	0.0292^{\diamond} (0.0004)	0.0270^{\diamond} (0.0003)
safe assets			0.0147^{\diamond} (0.0003)	0.0117^{\diamond} (0.0003)
constant	2.3263^{\diamond} (0.2062)	1.1514^{\diamond} (0.2079)	1.1309^{\diamond} (0.2165)	1.1718^{\diamond} (0.3211)
Observations Year FE Industry & Occupation FE	10,243 No No	10,239 Yes No	10,239 Yes No	7,606 Yes Yes
ME for women at age 30	-0.1414 ^{\displaystart} (0.0046)	-0.0846 ^{\disp} (0.0040)	-0.0583° (0.0048)	-0.0548° (0.0058)
ME for women at mean age (47)	-0.0572^{\diamond} (0.0024)	-0.0308^{\diamond} (0.0021)	-0.0142° (0.0018)	-0.0263° (0.0031)
ME for women at age 65	0.0282^{\diamond} (0.0041)	0.0239° (0.0041)	0.0307^{\diamond} (0.0040)	0.0078^{\diamond} (0.0027)

Notes: Estimations are based on OLS on the sample of individuals who live in households with no spouse present. Source: SCF waves 1989 until 2016. SMP = Stock Market Participation. $single\ woman$ is a dummy indicating that the household head is a woman. $high\ education$ indicates that the household head has more than 12 years of education. $safe\ assets$ refers to all net worth that is not invested in risky assets. "ME" indicates the marginal effect of being a woman at the respective age. Robust standard errors in parentheses, \diamond p<0.05.

Table 10: Regression Coefficients & Marginal Effects - Conditional Risky Share of Singles

	(1) Cond. Share	(2) Cond. Share	(3) Cond. Share	(4) Cond. Share
single woman	-0.0120° (0.0033)	-0.0021 (0.0067)	-0.0196 (0.0170)	-0.0113 (0.0169)
single woman * age	-0.0009° (0.0001)	-0.0009^{\diamond} (0.0002)	-0.0008^{\diamond} (0.0004)	-0.0011° (0.0004)
age	0.0273 (0.0145)	0.0428^{\diamond} (0.0147)	0.0305^{\diamond} (0.0117)	0.0388^{\diamond} (0.0105)
$age^2 * 100$	-0.0628^{\diamond} (0.0293)	-0.0969^{\diamond} (0.0294)	-0.0587° (0.0242)	-0.0763° (0.0214)
$age^3 * 10000$	0.0445^{\diamond} (0.0193)	0.0684° (0.0193)	0.0391^{\diamond} (0.0162)	0.0524° (0.0142)
high education		0.0282^{\diamond} (0.0022)	0.0542^{\diamond} (0.0032)	0.0333^{\diamond} (0.0023)
no. of HH members		-0.0238^{\diamond} (0.0017)	-0.0235° (0.0012)	-0.0225° (0.0015)
non-asset income		0.0055^{\diamond} (0.0006)	0.0055^{\diamond} (0.0006)	0.0079^{\diamond} (0.0009)
safe assets			-0.0380° (0.0006)	-0.0389° (0.0007)
constant	-0.0186 (0.2340)	-0.3918 (0.2321)	0.0902 (0.1873)	-0.0957 (0.1670)
Observations Year FE Industry & Occupation FE	4,285 No No	4,285 Yes No	4,285 Yes No	3,774 Yes Yes
ME for women at age 30	-0.0400° (0.0016)	-0.0300° (0.0028)	-0.0440° (0.0064)	-0.0444° (0.0068)
ME for women at mean age (49)	-0.0574° (0.0031)	-0.0466^{\diamond} (0.0029)	-0.0592° (0.0026)	-0.0639^{\diamond} (0.0031)
ME for women at age 65	-0.0726^{\diamond} (0.0049)	-0.0616^{\diamond} (0.0049)	-0.0725° (0.0072)	-0.0830° (0.0070)

Notes: Estimations are based on OLS on the sample of individuals who live in households with no spouse present. Source: SCF waves 1989 until 2016. Cond. Share = risky share conditional on participation. $single\ woman$ is a dummy indicating that the household head is a woman. $high\ education$ indicates that the household head has more than 12 years of education. $safe\ assets$ refers to all net worth that is not invested in risky assets. "ME" indicates the marginal effect of being a woman at the respective age. Robust standard errors in parentheses, \diamond p<0.05.

B Housing

The focus of this paper is on risky financial assets which is why I abstract from modeling housing explicitly. However, housing constitutes a large share of households' portfolios and affects stock market behavior.²⁶ For the current analysis, abstracting from housing is a problem if either housing choices directly map into portfolio behavior (and hence, the gender investment gap is in fact a gender housing gap) or if housing differentially affects portfolio choices by gender, i.e., if housing is an important driver of the gender investment gap itself.

To explore whether either of these issues is present in the data, I conduct two exercises: first, if portfolio choices are a direct mapping of housing decisions, I would expect the life-cycle profiles of housing variables to closely follow those in Figures 1a to 1c. Figure 11 displays singles' life-cycle profiles of homeownership rates, housing wealth (henceforth: "HW"), and housing wealth-to-income ratio (henceforth: "HI"). Housing refers to the primary residence. For all three variables, I do not find any significant differences between men and women despite significant gender gaps in equity shares both along the extensive and intensive margin.

Figure 11: Life-Cycle Profiles of Housing Patterns (Singles)



Notes: Figure 11 plots life-cycle profiles of the homeownership rate, gross housing wealth, and housing wealth-to-income ratio for single men and single women, including 95% confidence intervals. Housing refers to the primary residence. Data is from the waves 1989 until 2016 of the Survey of Consumer Finances (SCF).

Second, if housing is an important driver of the gender investment gap itself, the gender gap in equity shares should differ by housing tenure. To test for this possibility, Figure 12a

²⁶ Two of the first papers to introduce housing in a model of portfolio choice were Cocco (2005) and Yao and Zhang (2005). Since then, there has been a large and ongoing literature on housing and portfolio choices, see for example Flavin and Yamashita (2011), Chetty, Sandor, and Szeidl (2017), or Paz-Pardo (2024).

plots the equity share of single homeowners and single non-homeowners (renters) over their life-cycle, separately by gender. I find that gender differences in equity shares (i.e., the gap between black and orange lines) are very similar for homeowners and renters. To further illustrate this finding, Figure 12b plots the gender investment gap for renters and owners by age. Both lines are not statistically significant different from one another, reassuring that housing does not differently affect portfolio choices of single men and single women.

Owners Renters

(b) Gender Investment Gap

Figure 12: Gender Gaps in Equity Shares by Housing Tenure

Notes: Figure 12a plots singles' life-cycle profiles of equity shares by gender and housing tenure. Figure 12b plots the gender gap in equity shares for homeowners and renters, respectively. The gender gap in Figure 12b is defined as the average equity share of single men minus the average equity share of single women at the respective age, i.e., the difference between black and orange lines in Figure 12a. Data is from the waves 1989 until 2016 of the Survey of Consumer Finances (SCF).

C Model Estimation – First Stage

Women (owner)

Women (renter)

(a) Equity Shares

C.1 Income Process Estimation – Stochastic Component

I estimate the stochastic component of the income process by the minimum distance estimator as in Guvenen (2009). I assume the unexplained part of the income process (that is, the residual term ϵ_{ij} from the income equation) to follow a persistent-transitory process which depends on the aggregate state Ω :

$$\tilde{y}_{ij} = z_{ij} + \epsilon_{\tilde{y}ij} \quad \text{with} \quad z_{ij} = \begin{cases} \mu_z^{\text{boom}} + \rho_{zi} z_{i,j-1} + \nu_{zij} & \text{if } \Omega = b \text{ with probability } (1 - p_{\text{rec}}) \\ \mu_z^{\text{rec}} + \rho_{zi} z_{i,j-1} + \nu_{zij} & \text{if } \Omega = r \text{ with probability } p_{\text{rec}} \end{cases}$$

Abstracting from the state-dependent mean μ_z , I need to estimate three parameters which are allowed to vary by gender and marital status: the persistence parameter ρ_z , the variance of the persistent shock $\sigma_{\epsilon_y}^2$, and the variance of the transitory shock $\sigma_{\nu_z}^2$. To do so, I minimize the distance between the covariance-variance matrices of the income process in the data and their theoretical counterparts under the assumption that $Var(z_{-1}) = 0$. In addition, note that the PSID collects data every two years after 1997 while the model is written in annual frequency. To account for this inconsistency, I linearly interpolate income for individuals that I observe in two consecutive waves for the missing year in which no PSID data was collected. I run four different estimations for married men, married women, single men, and single women. Table 2 in the main text displays the results.

Human Capital Returns. The mean of the persistent part of (stochastic) income μ_z depends on the aggregate state and hence, governs the correlation between stock market returns and income realizations. I set its value during recessions μ_z^{rec} to be small enough such that the correlation between human capital and stock returns is positive but does not exceed values from previous literature.²⁷ As in Huggett and Kaplan (2016), I define the return to human capital as next period's human capital value plus net earnings (i.e., the dividend of human capital), divided by the current period's value of human capital: $R_{j+1}^h = \frac{v_{j+1} + e_{j+1}}{v_j}$.

In turn, again following Huggett and Kaplan (2016), the value of human capital v is defined as households' expected discounted net earnings, with discounting done using the household's stochastic discount factor. Thus, the value of human capital for a household with gender i, age j, education θ , asset cash-on-hand a, and productivity realization \tilde{y} reads as:²⁸

$$v(i, j, \theta, a, \tilde{y}) = \mathbb{E}_{k=j+1}^{J} m_{j,k} e_k(i, j, \theta, a, \tilde{y})$$

The value for $\mu_z^{\rm boom}$ is then automatically determined through the stationary condition for the income process: $\mu_z^{\rm boom} = \left(\frac{-p_{\rm rec}}{1-p_{\rm rec}}\right)\mu_z^{\rm rec}$.

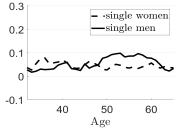
²⁸ Because the labor income processes differ between married and single individuals, I assume for simplicity that singles take expectations only over the states when they remain single when computing human capital values.

where $e_k(i, j, \theta, a, \tilde{y})$ denote expected net earnings in period k. The term $m_{j,k}$ is the house-hold's stochastic discount factor. Let X^j summarize household's state space in period j. I then define the stochastic discount factor $m_{j,k}$ as:

$$m_{j,k} = \beta P(X^k | X^j) \frac{\partial U(c^*) / \partial c_k(X^k)}{\partial U(c^*) / \partial c_z(X^j)}$$

The operator $P(X^k|X^j)$ denotes the likelihood to end up in state X^k in period k, given that the household is in state X^j today. Figure 13 plots the correlation between human capital and stock returns for single men and single women over their life-cycle in my model. While the correlation is positive, it is below the estimates in Huggett and Kaplan (2016) who find values of around 0.3 to 0.5. However, there are several key model ingredients that differ between their and my framework. First, Huggett and Kaplan (2016) do not impose any fixed cost of stock market participation. Second, while they consider the sample of (both married and unmarried) males, I restrict the analysis to singles who are generally exposed to more labor income risk (e.g. because they cannot pool individual income streams). Finally, Huggett and Kaplan (2016) introduce pension payments that depend on the aggregate component of earnings, whereas these two factors are uncorrelated in my framework. All those elements contribute to agents in my framework being less willing to invest in the risky asset and hence, a smaller correlation between human capital and stock returns is needed to match empirical equity shares.

Figure 13: Correlation: Human Capital and Stock Returns



Notes: Figure 13 plots the correlation between human capital and stock returns by age for single men and single women.

C.2 Income Process – Deterministic Component

Table 11: Regression Coefficients for Income Estimation (Deterministic Component)

	(1) First Stage	(2) Second Stage	(3) First Stage	(4) Second Stage
	Couples		Singles	
high educ.		0.5528° (0.0174)		0.4496° (0.0259)
woman		-3.9130° (0.0328)		-0.7061° (0.0246)
woman*high educ.		-0.3021° (0.0421)		0.1156° (0.0322)
age	0.0798^{\diamond} (0.0165)		0.0596^{\diamond} (0.0115)	
age^2*100	-0.0884° (0.0173)		-0.0734° (0.0113)	
age*woman	0.0523^{\diamond} (0.0046)		0.0109° (0.0380)	
constant	7.5471^{\diamond} (0.3838)	1.7195° (0.0136)	9.6027^{\diamond} (0.2730)	0.1330° (0.0200)
Observations Number of unique indiv.	76,926 10,705	76,926	17,390 3,608	17,390

Notes: Estimations are based on (fixed-effect) OLS regressions from PSID Data, waves 1989-2017. Corresponding Figure is Figure 2 in the main text. Dependent variable of first stage: inverse hyperbolic sine transformation of annual non-asset income (labor income, social security income, and transfers). In waves where social security income and transfers are not available separately for head and spouse, I use the combined social security and transfer income and assign it 50-50 to both spouses. For singles, I add labor income, social security benefits, and transfers from other household members. For couples, I split income from other household members 50-50 between spouses. Dependent variable of second stage: fixed effects plus residual from first stage. $high\ educ$. is a dummy equal to one if the individual has more than 12 years of schooling; woman is a dummy indicating if the individual is a woman; Robust standard errors in parentheses, $\diamond p < 0.05$.

C.3 Marriage and Divorce Probabilities

Table 12: Regression Coefficients for Marriage and Divorce Probabilities

	(1)	(2)
	Marriage Prob.	Divorce Prob.
woman	-0.3196^{\diamond}	
	(0.0735)	
age	-0.0589*	-0.0443
	(0.0038)	(0.0054)
1 > 1997	0.3853^{\diamond}	0.5796^{\diamond}
	(0.0662)	(0.0959)
high educ. (head)	0.0768	-0.3988
	(0.0722)	(0.1151)
high educ. (spouse)		-0.0894
,		(0.1110)
constant	0.1257	-1.5719
	(0.1579)	(0.2506)
Observations	13,554	18,178

Notes: Estimations are based on Logit regressions from PSID Data, waves 1989-2017. Dependent variable: likelihood of getting married (resp. divorced) within the next wave, conditional on not being married (resp. being married) today. The age of a couple refers to the household head. For education within a couple, head refers to the husband and spouse refers to the wife. Singles are always labeled as heads. high educ. is a dummy equal to one if the individual has more than 12 years of schooling; woman is a dummy indicating if the individual is a woman; $\mathbbm{1} > 1997$ indicates observations that were interviewed after 1997 to account for changing frequency of the PSID. Robust standard errors in parentheses, \diamond p<0.05.

D Model Results

D.1 Solution Method & Simulation

For a given set of parameters, I solve the model using backward iteration. Agents die with certainty in the terminal period (T) and I can directly solve for their optimal consumption/saving combination for each point in the state space via grid search in period T. Having found the optimal choices in period T, I iterate one period backward and solve for the optimal

choices in period T-1 and so forth. During retirement, I solve the problem independently for couples, single men, and single women. During working age, I need to take into account that individuals may switch marital status and hence, the continuation value of couples depends on the solution of the single problem (and vice versa).

After having solved for the policy functions, I simulate the model for a large number of individuals over their life-cycle. At age 30, I assign each individual an initial level of wealth, education, and marital status. Next, I simulate a chain of the aggregate state, marital transitions, labor income shocks, and asset return realizations (that, importantly, depend on each other) and assign each individual a certain chain of these shock processes. I simulate the model for 25,000 men and 25,000 women who may switch marital status throughout their working life. Once a single gets married, his or her partner is assigned from "outside" the model. Likewise, if the couple gets divorced, that partner again disappears from the simulation. Lastly, I construct the moments for each simulation, compute the objective function using the weighting matrix, and find the statistic of the model fit \mathcal{L} . Given the computational complexity of the structural framework, I can only repeat this procedure for a limited number of runs. Therefore, I use the TikTak global optimization algorithm (Guvenen and Ozkan, 2021) to find a sequence of 70 sobol points at which I evaluate the model. Next, I further improve the model fit by searching within a narrow bound of parameters around the before found minimum.

D.2 Further Results on Model Fit

Figure 14 reports the model fit for couple households, which are left entirely untargeted in the calibration exercise. While the model matches the equity share of couples over the life-cycle well (Figure 14a), it underpredicts their participation rate early in life. Moreover, it misses the fast asset accumulation of couples.

The faster empirical asset accumulation can arise from various sources that go beyond the focus of my paper and are therefore absent in the model. For example, couples have on average

more children than singles which may induce them to save for their children's education expenses. In addition, couples are more likely to be homeowners, generating high saving rates. Regardless of the underlying mechanism, the results of my paper do not depend on the model's ability to match the life-cycle profiles of couples: in a previous version, I improved the fit for couples by allowing their preference parameters (discount factor, coefficient of risk aversion, and stock market participation cost) to differ from those of singles, which did not alter the main results.

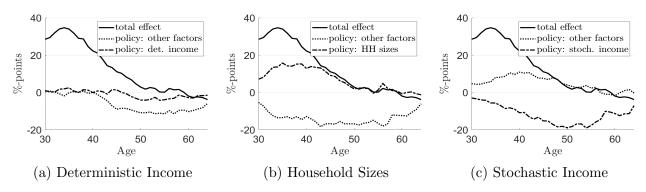
Participation Rate -model data 0.4 Equity Share 0.3 0.2 0.1 0 30 0 30 40 50 60 40 50 60 (a) Equity Share (b) Participation Rate (000s) Assets in 2007 \$ 1000 Equity Share 500 0 30 30 40 50 50 60 40 60 Age (c) Conditional Risky Share (d) Net Worth

Figure 14: Model Fit of Couples

Notes: Figure 14 plots the model fit for the unconditional equity share, participation rate, conditional risky share, and net worth for couple households. The solid lines show the data (including 95% confidence bands, as plotted in Figure 1) whereas the dashed lines display the simulated life-cycle profiles generated from the model.

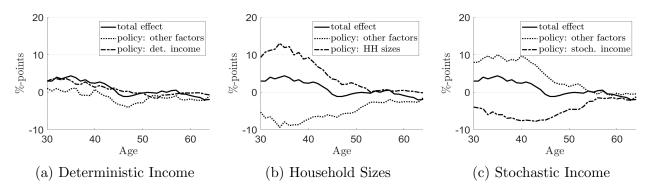
D.3 Composition vs. Policy Effect – Further Results

Figure 15: Decomposition of Policy Effect – Participation Rates



Notes: Figure 15 illustrates the importance of gender heterogeneity in deterministic income, household sizes, and stochastic income for the policy effect in participation rates. The solid lines refer to the total gender investment gap, the dashed-dotted lines show the part of the policy effect that can be attributed to the respective channel, whereas the dotted lines report the importance of all remaining channels (as listed in Table 5).

Figure 16: Decomposition of Policy Effect – Conditional Risky Shares



Notes: Figure 16 illustrates the importance of gender heterogeneity in deterministic income, household sizes, and stochastic income for the policy effect in conditional risky shares. The solid lines refer to the total gender investment gap, the dashed-dotted lines show the part of the policy effect that can be attributed to the respective channel, whereas the dotted lines report the importance of all remaining channels (as listed in Table 5).